

Lecture 34 - Bipolar Junction Transistor

May 2, 2007

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Reading material:

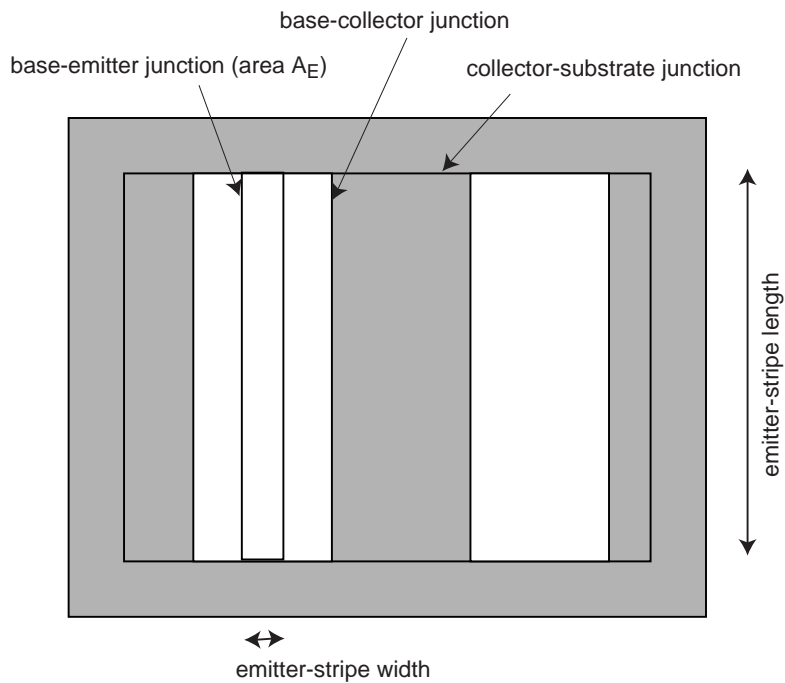
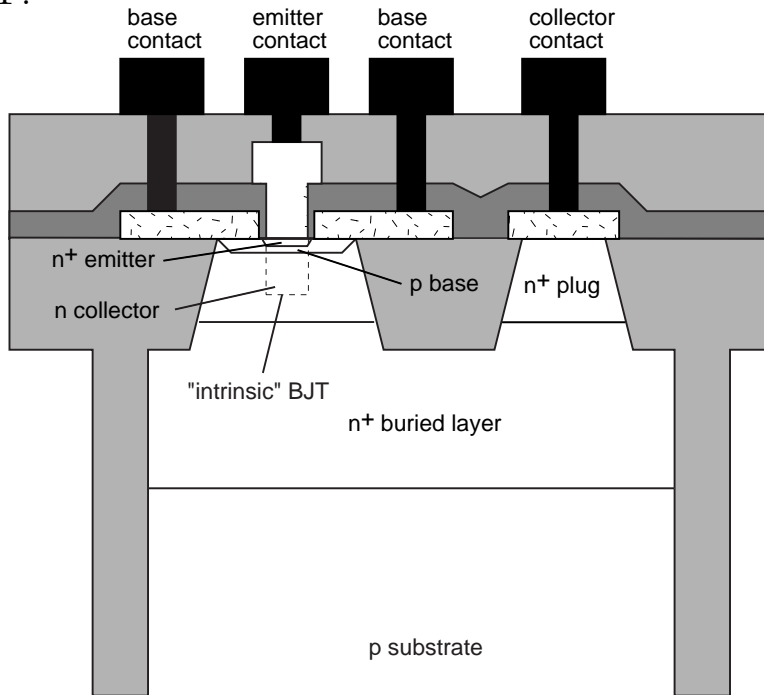
del Alamo, Ch. 11, §§11.1, 11.2 (11.2.1)

Key questions

- How does a bipolar junction transistor look like?
- How does a BJT basically work?
- Can we derive a first order model for I_C and I_B in forward-active regime?

1. The ideal BJT

Modern BJT:

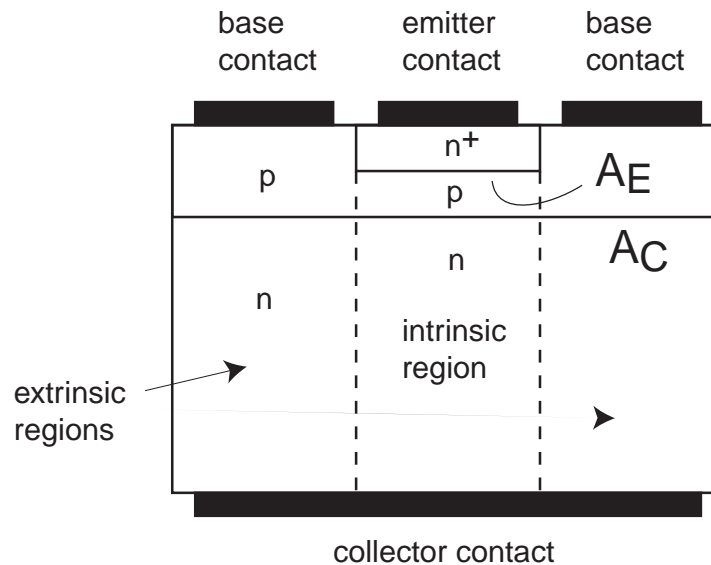


BJT basically consists of two neighbouring pn junctions back-to-back:

- close enough that minority carriers interact (negligible recombination in base)
- far apart enough that depletion regions don't interact (no "punchthrough")

Uniqueness of BJT: high current drivability per input capacitance \Rightarrow fast \Rightarrow excellent for analog and front-end communications applications.

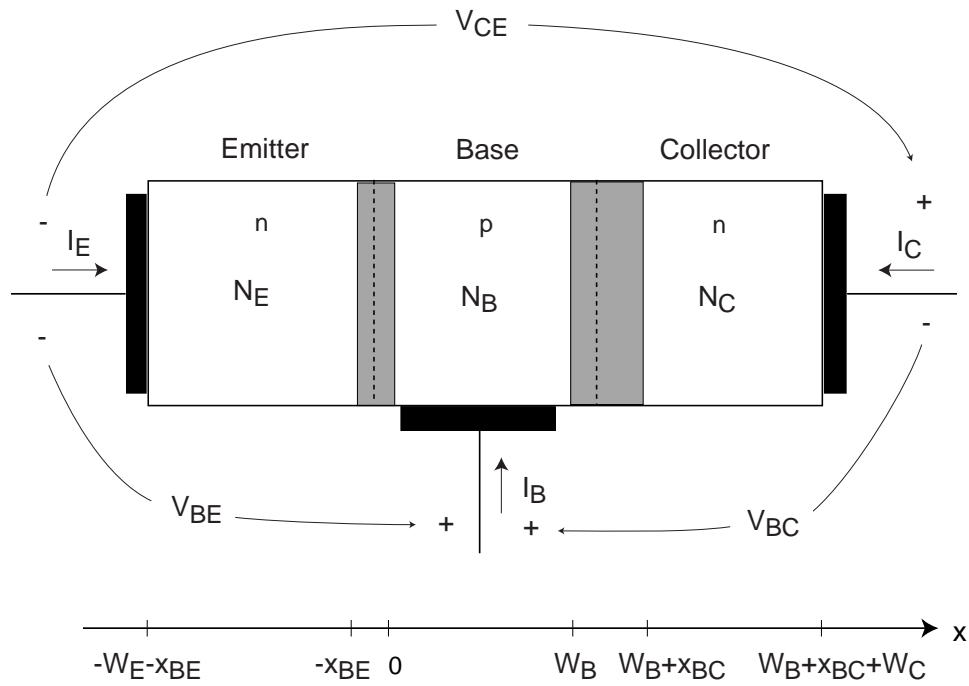
Ideal BJT:



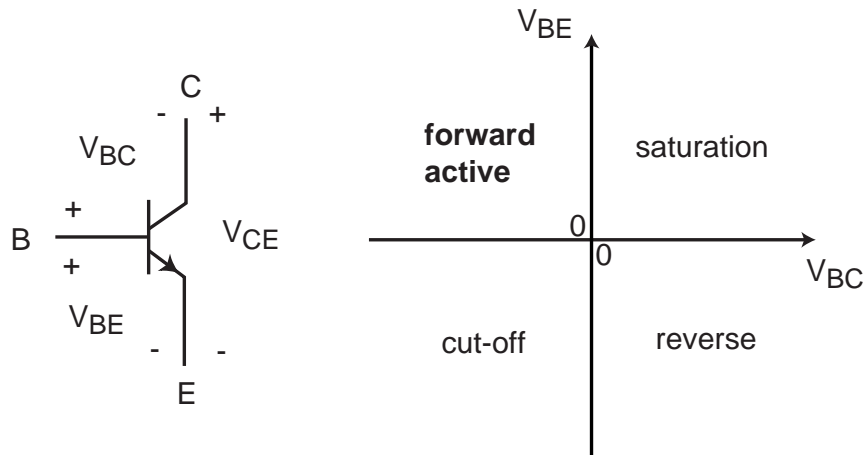
Ideal BJT simplifications:

- 1D.
- Uniform doping distributions.
- Minority carrier G&R in intrinsic base is negligible.
- Emitter, extrinsic base and collector also assumed "short" from minority carrier point of view.
- Low-level injection.
- QNR thicknesses independent of V_{BE} and V_{BC} .
- Ignore sidewall effects.
- No parasitic resistances.
- Ignore substrate.

Simplified 1D model of intrinsic device:

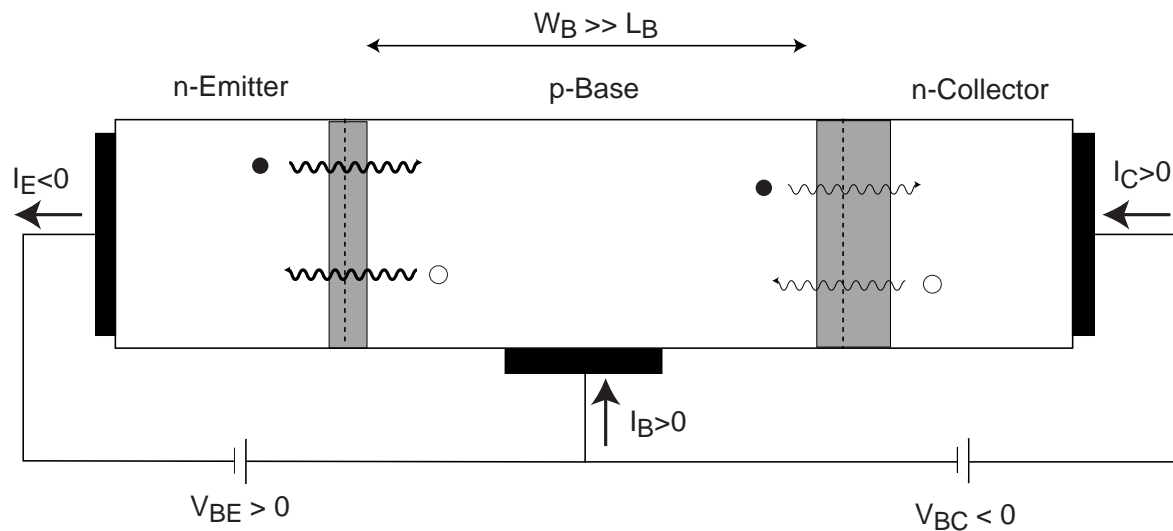


Regimes of operation:



2. Current-voltage characteristics of ideal BJT

- Basic operation in forward active regime:
- Two junctions back-to-back:

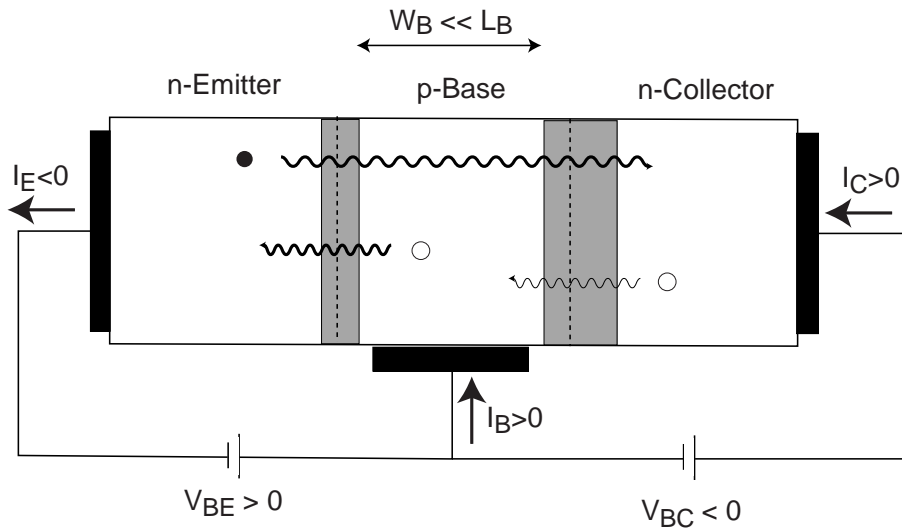


$V_{BE} > 0 \Rightarrow$ injection of electrons from E to B
injection of holes from B to E

$V_{BC} < 0 \Rightarrow$ extraction of electrons from B to C
extraction of holes from C to B

$$I_B \simeq -I_E \gg I_C$$

- *Transistor effect*: electrons injected from E to B, extracted by C

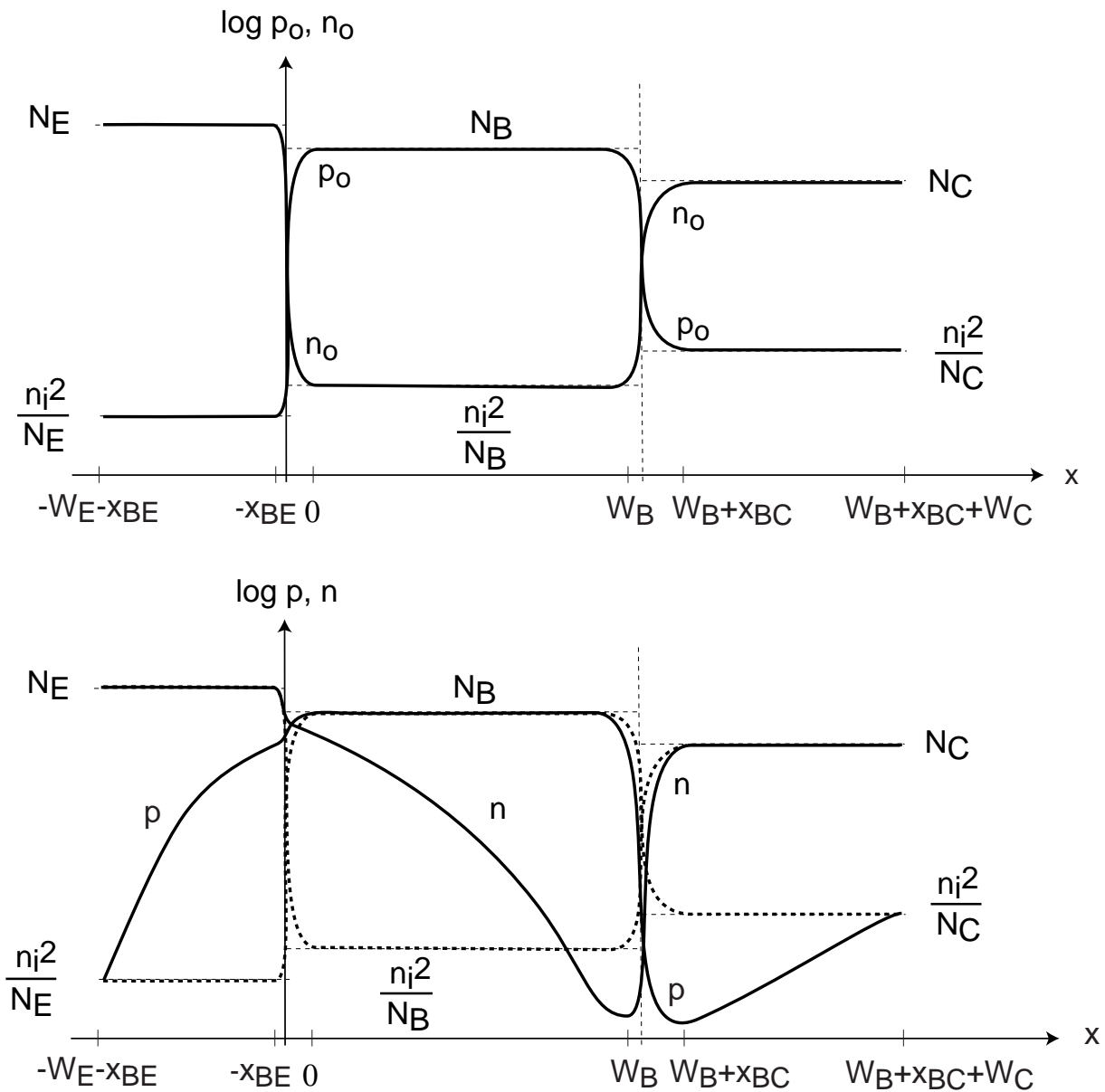


$$I_C \simeq -I_E \gg I_B$$

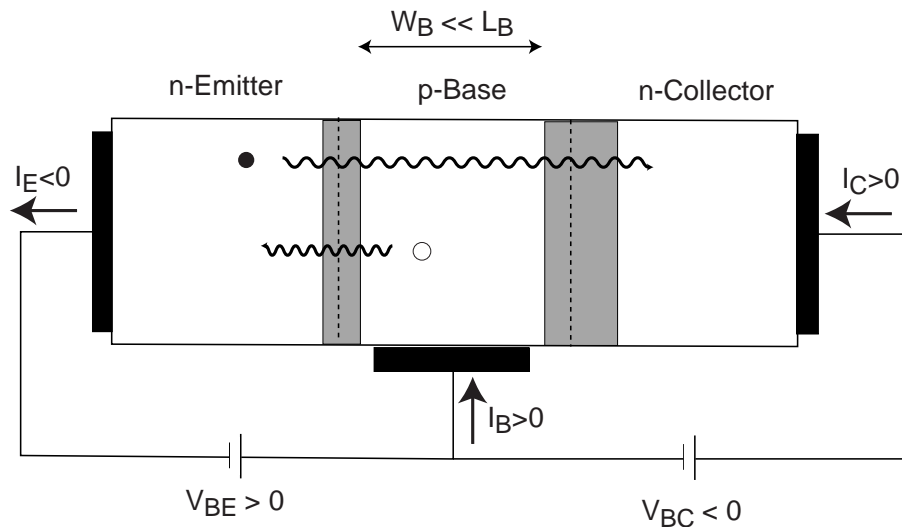
In forward-active regime:

- V_{BE} controls I_C ("transistor effect")
- I_C independent of V_{BC} ("isolation")
- price to pay for control: I_B

Carrier profiles in TE and FAR:



Dominant current paths in forward active regime:



I_C : electron injection from E to B and collection into C

I_B : hole injection from B to E

$$I_E = -I_C - I_B$$

Key dependencies (choose one):

I_C on V_{BE} : $e^{qV_{BE}/kT}$, $1/\sqrt{V_{BE}}$, none, other

I_C on V_{BC} : $e^{qV_{BC}/kT}$, $1/\sqrt{V_{BC}}$, none, other

I_B on V_{BE} : $e^{qV_{BE}/kT}$, $1/\sqrt{V_{BE}}$, none, other

I_B on V_{BC} : $e^{qV_{BC}/kT}$, $1/\sqrt{V_{BC}}$, none, other

I_C on I_B : exponential, quadratic, none, other

In forward-active regime:

- V_{BE} controls I_C ("transistor effect")
- I_C independent of V_{BC} ("isolation")
- price to pay for control: I_B

Comparison with MOSFET:

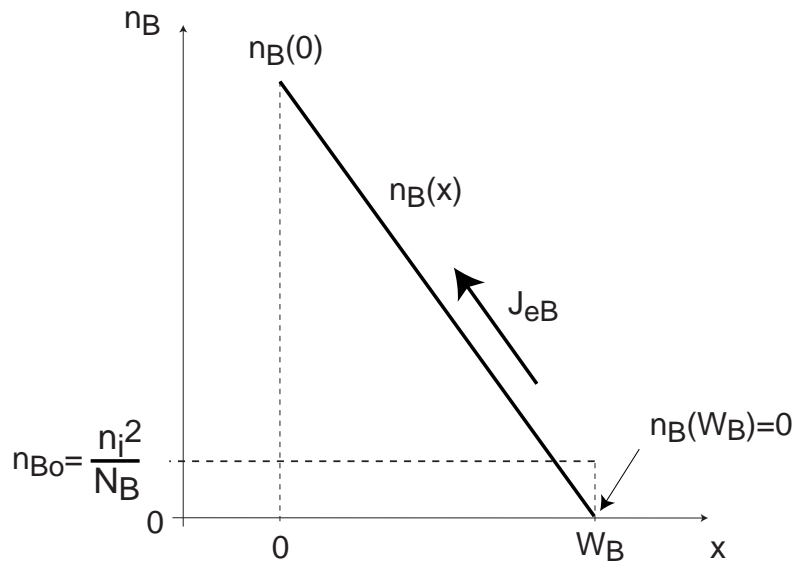
feature	ideal BJT in FAR	ideal MOSFET in saturation
controlling terminal	base	gate
controlled terminal	collector	drain
common terminal	emitter	source
functional dependence of controlled current	exponential	quadratic
DC current in controlling terminal	exponential	0

Figure of merit for BJT:

common-emitter current gain: $\beta_F = \frac{I_C}{I_B}$ (want big)

□ **Forward-active regime** ($V_{BE} > 0$, $V_{BC} < 0$)

• *Collector current*



Boundary conditions:

$$n_B(0) = n_{B0} \exp\left(\frac{qV_{BE}}{kT}\right), \quad n_B(W_B) = 0$$

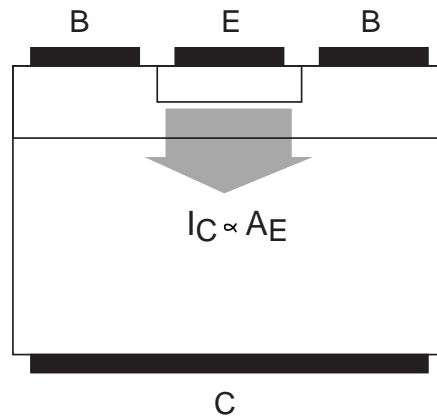
Electron profile:

$$n_B(x) = n_B(0) \left(1 - \frac{x}{W_B}\right)$$

Electron current density:

$$J_{eB} = qD_B \frac{dn_B}{dx} = -qD_B \frac{n_B(0)}{W_B}$$

Collector current scales with area of base-emitter junction A_E :



Collector terminal current:

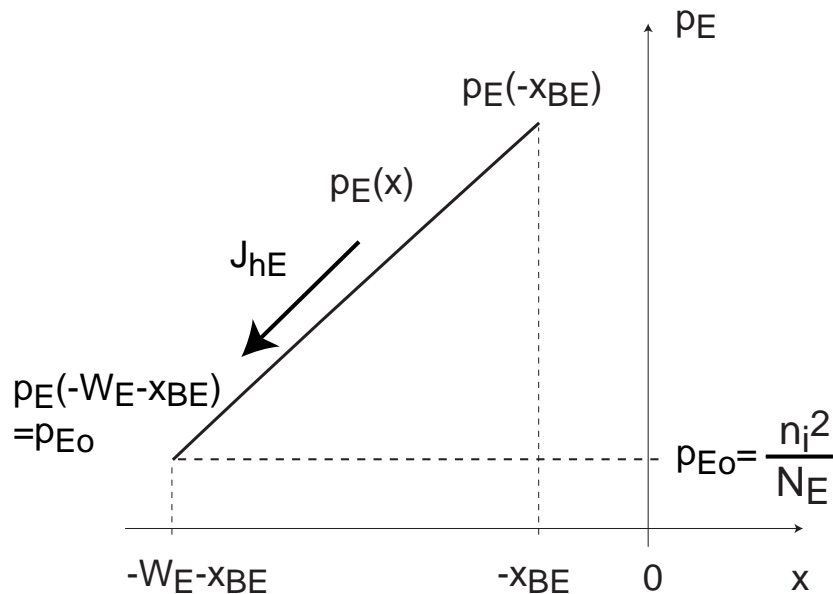
$$I_C = -J_{eB}A_E = qA_E \frac{n_i^2 D_B}{N_B W_B} \exp \frac{qV_{BE}}{kT}$$

or

$$I_C = I_S \exp \frac{qV_{BE}}{kT}$$

$I_S \equiv$ collector saturation current

- *Base current*: focus on hole injection and recombination in emitter (assume "short" or "transparent" and $S = \infty$ at surface)



Boundary conditions:

$$p_E(-x_{BE}) = p_{E0} \exp\left(\frac{qV_{BE}}{kT}\right), \quad p_E(-W_E - x_{BE}) = p_{E0}$$

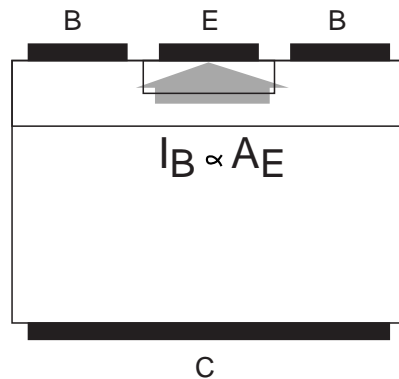
Hole profile:

$$p_E(x) = [p_E(-x_{BE}) - p_{E0}] \left(1 + \frac{x + x_{BE}}{W_E}\right) + p_{E0}$$

Hole current density:

$$J_{hE} = -qD_E \frac{dp_E}{dx} = -qD_E \frac{p_E(-x_{BE}) - p_{E0}}{W_E}$$

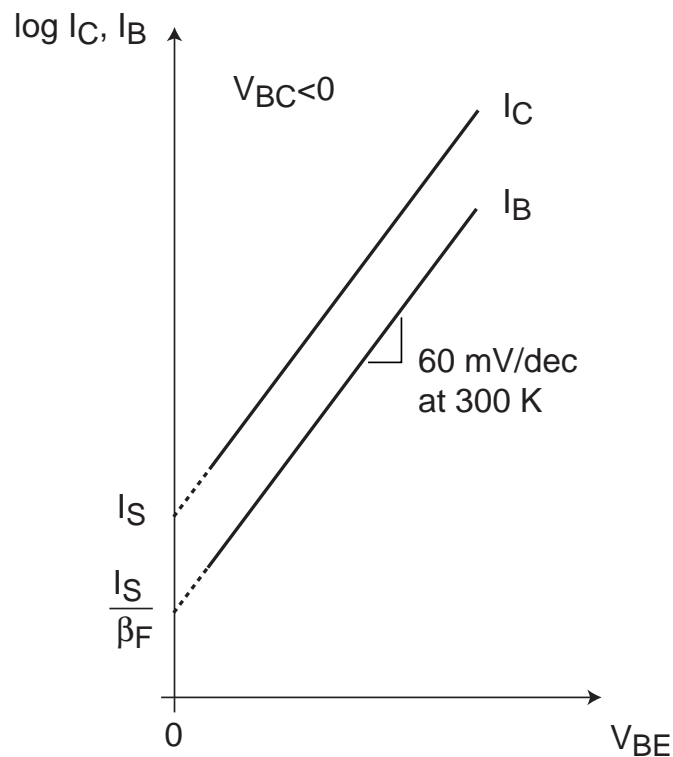
Base current scales with area of base-emitter junction A_E :

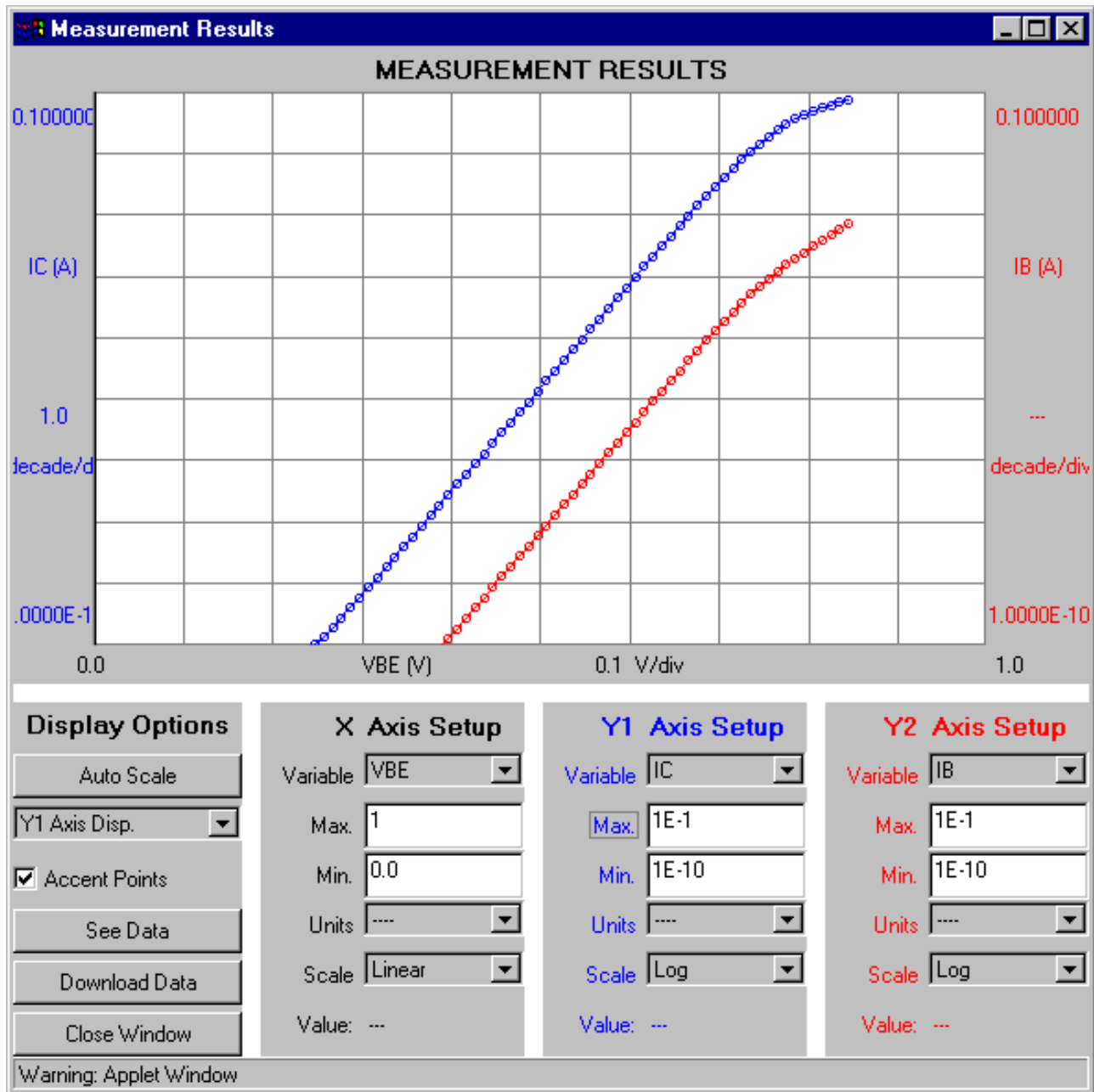


Base terminal current:

$$I_B = -J_{hE}A_E = qA_E \frac{n_i^2}{N_E} \frac{D_E}{W_E} \left(\exp \frac{qV_{BE}}{kT} - 1 \right) = \frac{I_S}{\beta_F} \left(\exp \frac{qV_{BE}}{kT} - 1 \right)$$

□ *Gummel plot*:





Key conclusions

- BJT is minority-carrier type device: in npn BJT in forward active regime: Emitter "injects" electrons into Base, Collector "collects" electrons from Base.
- I_C controlled by V_{BE} , but independent of V_{BC} (*transistor effect*):

$$I_C = I_S \exp \frac{qV_{BE}}{kT}$$

- Base injects holes into Emitter $\Rightarrow I_B$ depends only on V_{BE} :

$$I_B = \frac{I_S}{\beta_F} \left(\exp \frac{qV_{BE}}{kT} - 1 \right)$$