

## Homework 4

#### 4.1 Random graph models

**[15 points]** Replicate the "small-world" experiment numerically. Start with a regular  $k$ -nearest neighbors ring-graph, and then keep adding random links to this graph. Observe how the clustering coefficient and average shortest path-length behaves as a function of the link-probability (see python notebook).

Describe the results you obtain in 5 or less sentences.

**[15 points]** You have learned about the Barabasi-Albert preferential attachment model in the lectures. Here we will explore it computationally. Use `networkx` to construct these graph for varying parameters and report on the result you obtain (see python notebook).

**[30 points]** In this exercise you are going to explore the stochastic block model. As you have already seen in the class, this random model is defined as follows:

We consider an undirected network with  $n$  nodes, which are divided into 2 equally sized groups which we name class 1 and class 2. The probability of a link between two nodes is now given by  $p$  if the nodes are in the same class, and by  $q$  if the nodes are in two different classes.

Your task is to

- create this random graph model,
- create graphs with varying parameters, and
- use spectral clustering to see whether you can recover the blocks. For more details see the python notebook.

Describe your findings in 5 sentences or less.

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