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# 16.485: VNAV - Visual Navigation for Autonomous Vehicles

**Luca Carlone**

Lecture 20: Visual and  
Visual-Inertial Odometry



# Today

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- VO: **V**isual **O**dometry
- VIO: **V**isual-**I**nertial **O**dometry



## Visual Odometry

Part I: The First 30 Years and Fundamentals

Part II: Matching, Robustness, Optimization, and Applications

By Friedrich Fraundorfer and Davide Scaramuzza

## On-Manifold Preintegration for Real-Time Visual-Inertial Odometry

Christian Forster, Luca Carlone, Frank Dellaert, Davide Scaramuzza

**Abstract**—Current approaches for visual-inertial odometry (VIO) are able to attain highly accurate state estimation via nonlinear optimization. However, real-time optimization quickly becomes infeasible as the trajectory grows over time; this problem is further emphasized by the fact that inertial measurements come at high rate, hence leading to fast growth of the number of variables in the optimization. In this paper, we address this issue by preintegrating inertial measurements between selected keyframes into single relative motion constraints. Our first contribution is a *preintegration theory* that properly addresses the manifold structure of the rotation group. We formally discuss the generative measurement model as well as the nature of the rotation noise and derive the expression for the *maximum a posteriori* state estimator. Our theoretical development enables the computation of all necessary Jacobians for the optimization and a-posteriori bias correction in analytic form. The second contribution is to show that the preintegrated IMU model can be seamlessly integrated into a visual-inertial pipeline under the unifying framework of factor graphs. This enables the application of incremental-smoothing algorithms and the use of a *structureless* model for visual measurements, which avoids optimizing over the 3D points, further accelerating the computation. We perform an extensive evaluation of our monocular VIO pipeline on real and simulated datasets. The results confirm that our modelling effort leads to accurate state estimation in real-time, outperforming state-of-the-art approaches.

of monocular vision and gravity observable [1] and provides robust and accurate inter-frame motion estimates. Applications of VIO range from autonomous navigation in GPS-denied environments, to 3D reconstruction, and augmented reality.

The existing literature on VIO imposes a trade-off between accuracy and computational efficiency (a detailed review is given in Section II). On the one hand, filtering approaches enable fast inference, but their accuracy is deteriorated by the accumulation of linearization errors. On the other hand, full smoothing approaches, based on nonlinear optimization, are accurate, but computationally demanding. Fixed-lag smoothing offers a compromise between accuracy for efficiency; however, it is not clear how to set the length of the estimation window so to guarantee a given level of performance.

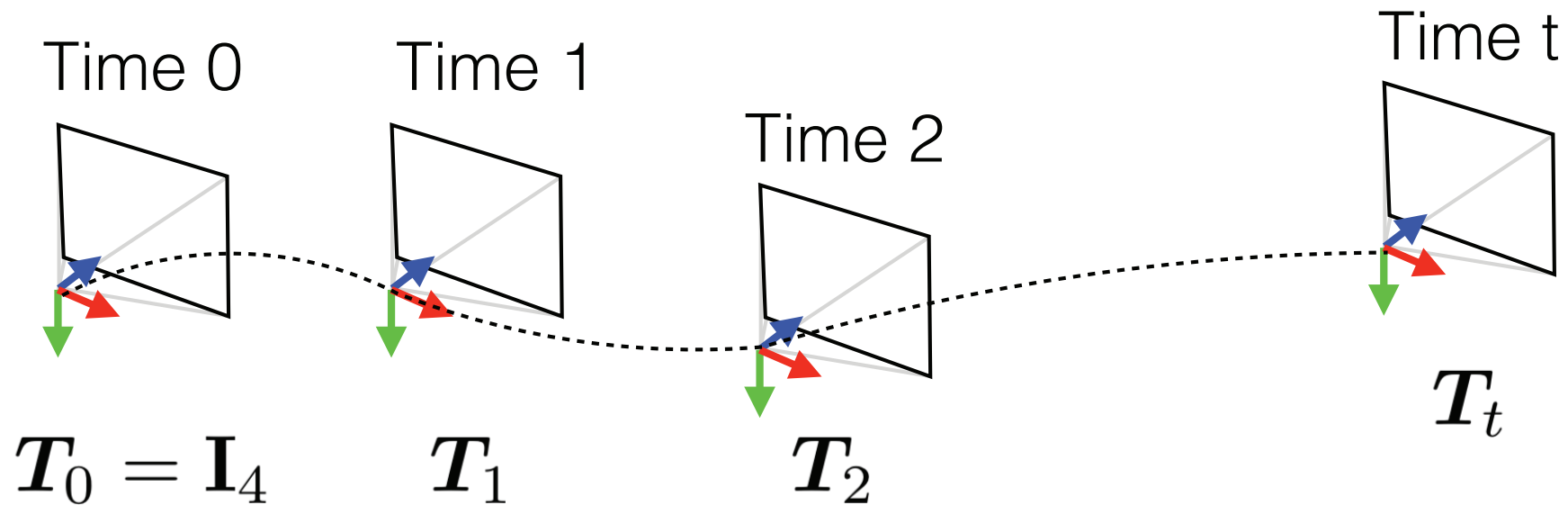
In this work we show that it is possible to overcome this trade-off. We design a VIO system that enables fast incremental smoothing and computes the optimal *maximum a posteriori* (MAP) estimate in real time. An overview of our approach is given in Section IV.

The first step towards this goal is the development of a novel preintegration theory. The use of *preintegrated IMU measurements* was first proposed in [2] and consists of combining

# Visual Odometry

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**odometry**: incremental motion estimation

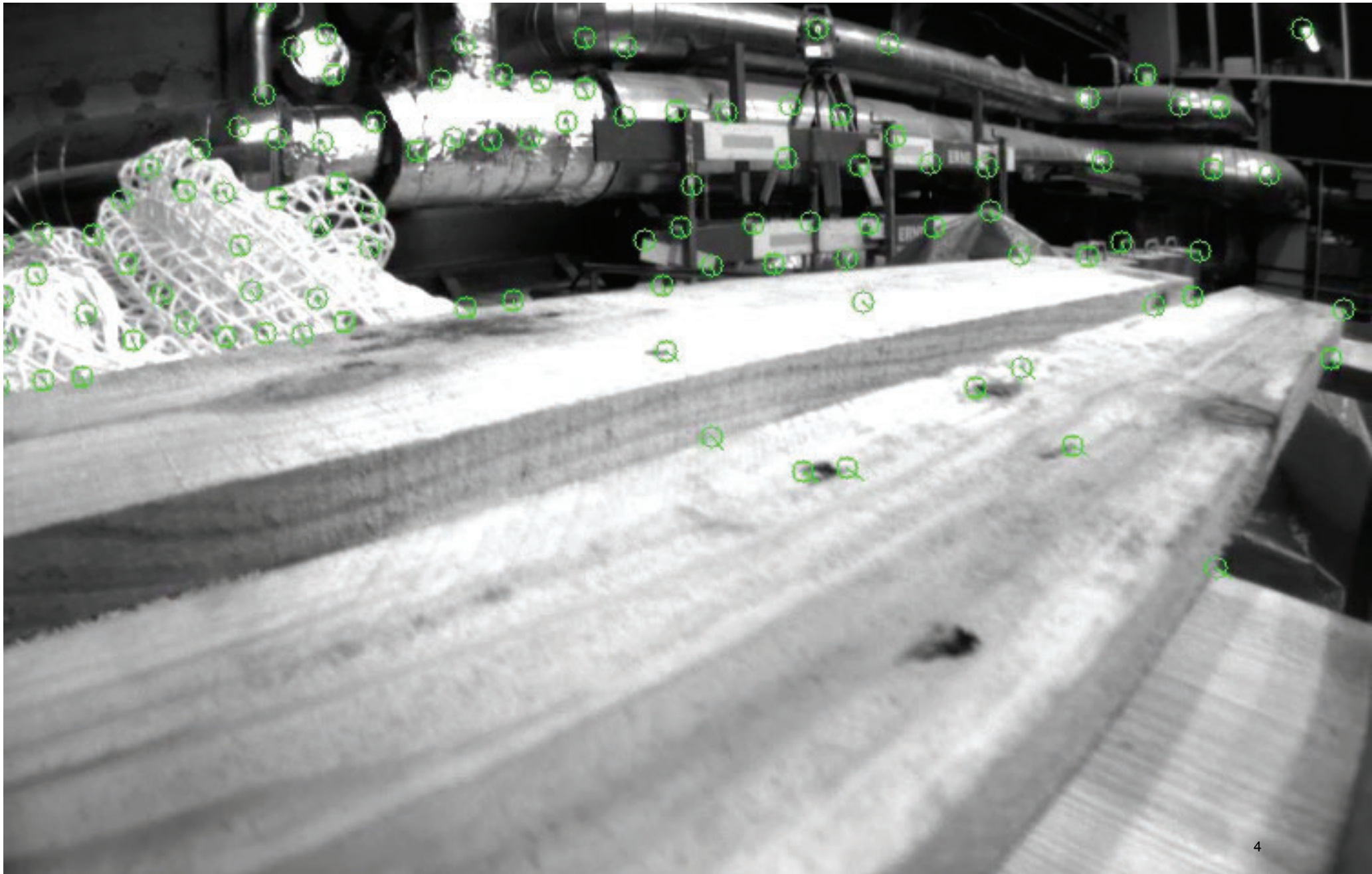


**Visual odometry (VO)**: motion estimation estimation based on cameras (monocular, stereo, RGB-D, ...)

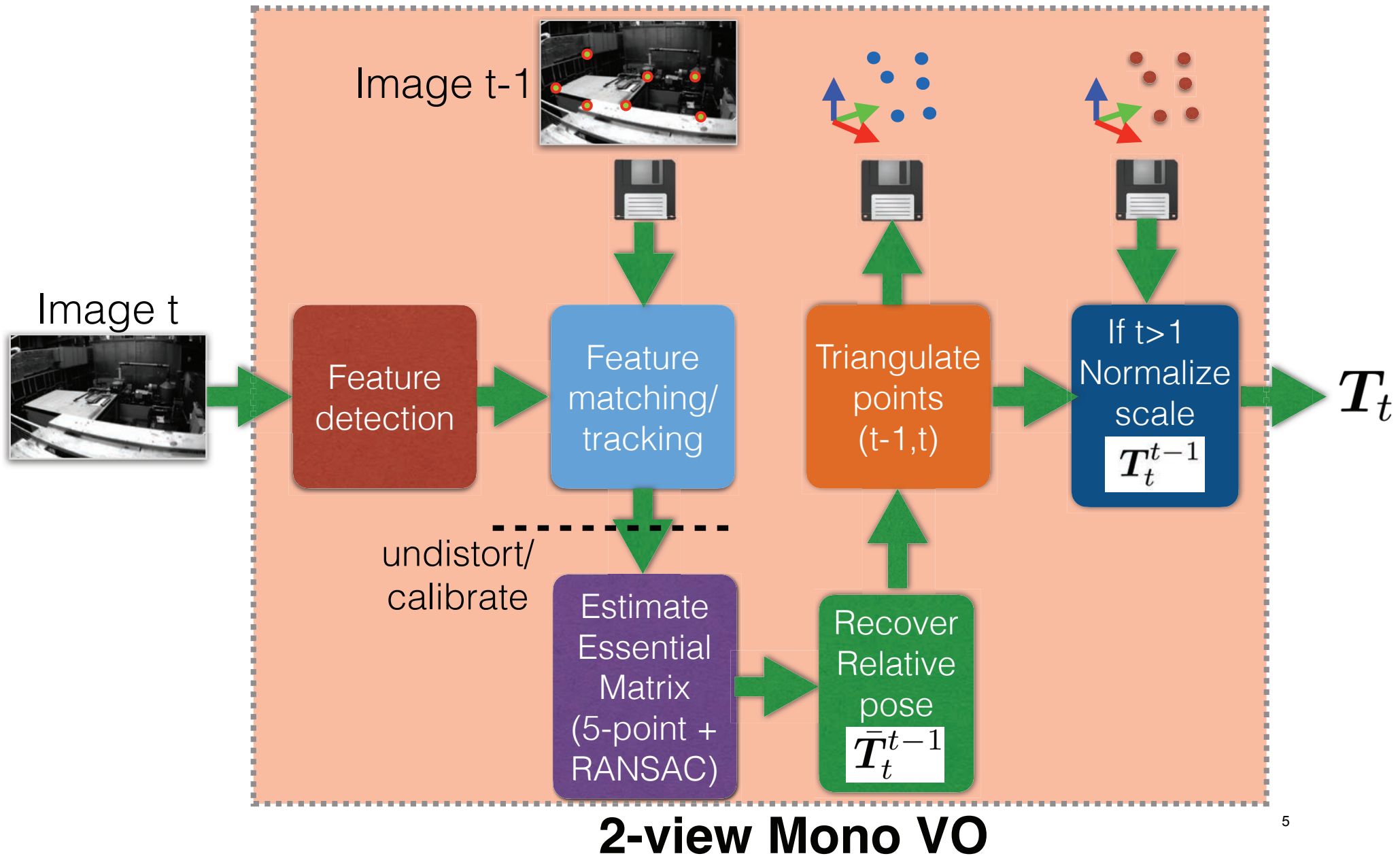
**others**: wheel odometry, inertial, visual-inertial



# Feature Tracking

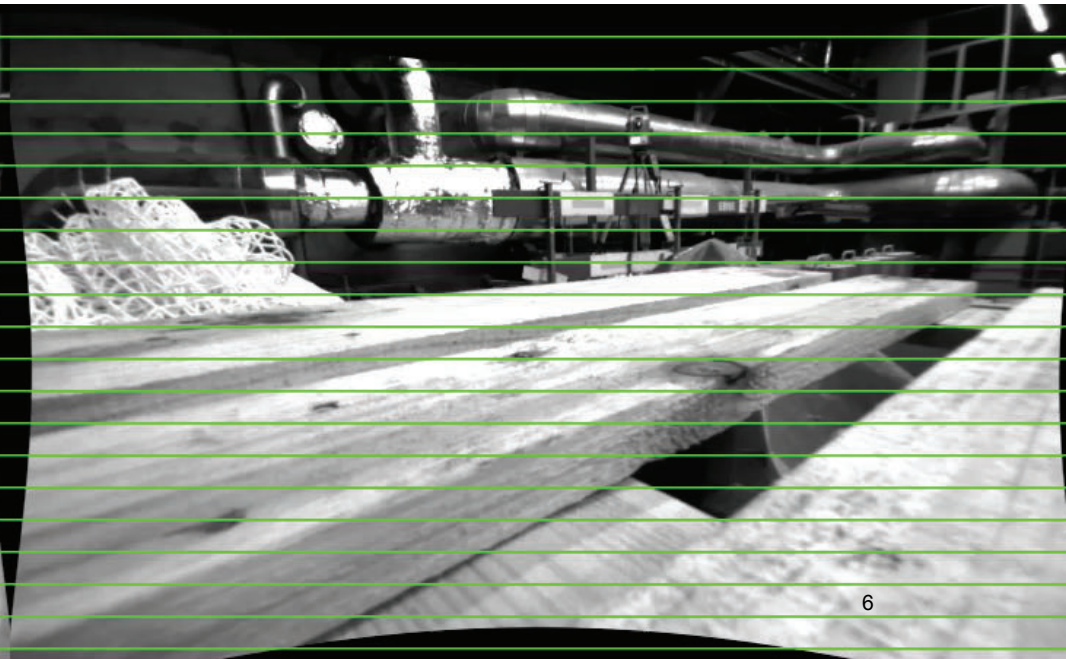
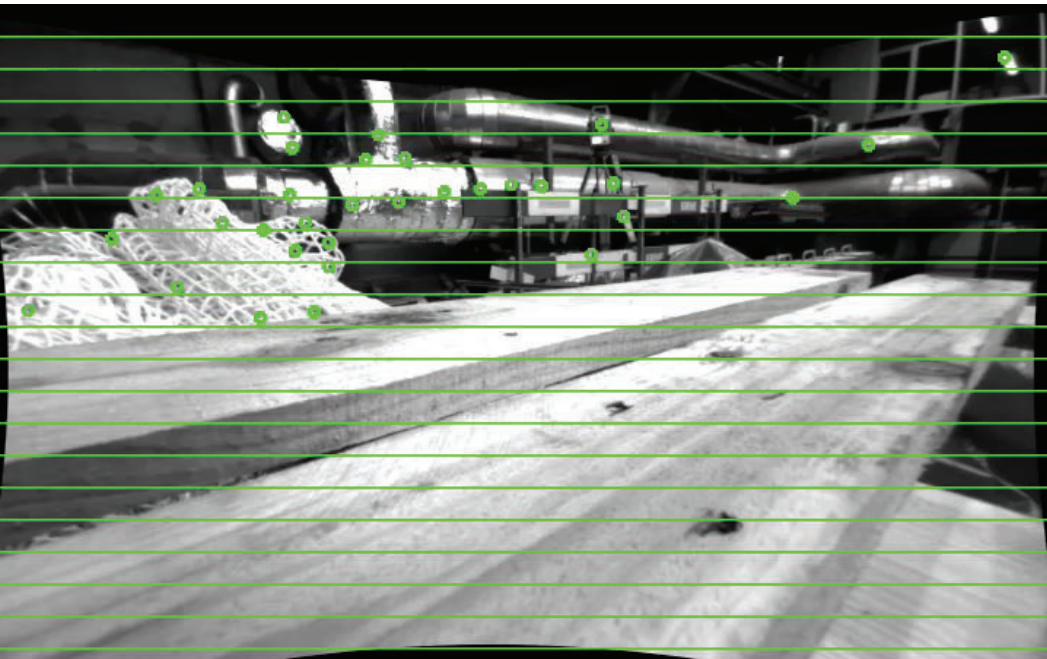
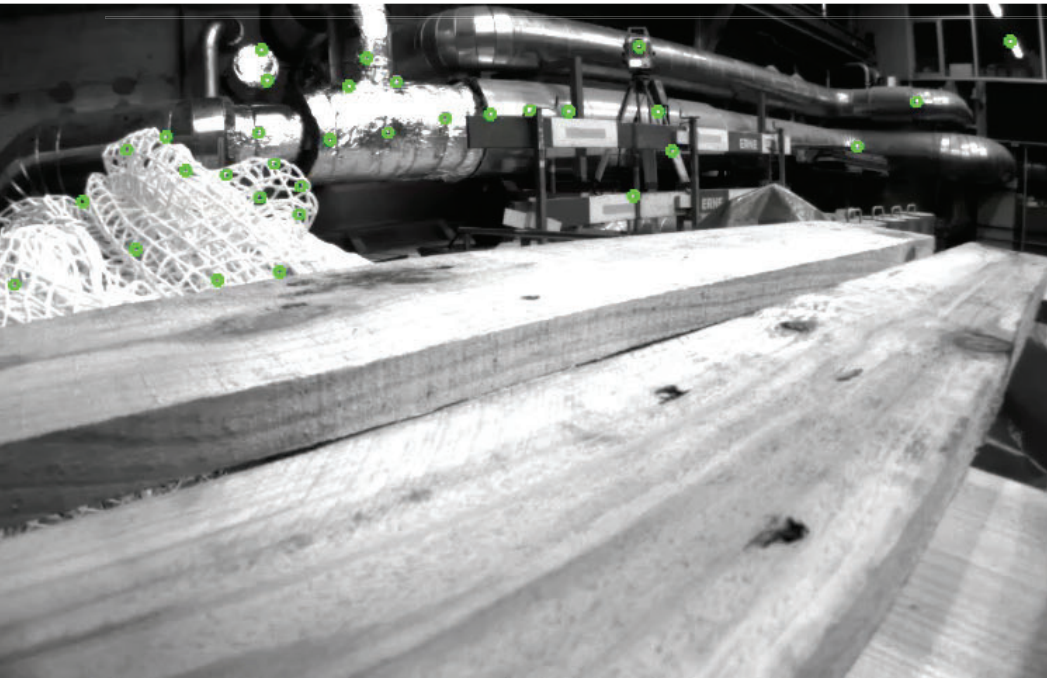


# Monocular VO with 2D-2D Correspondences

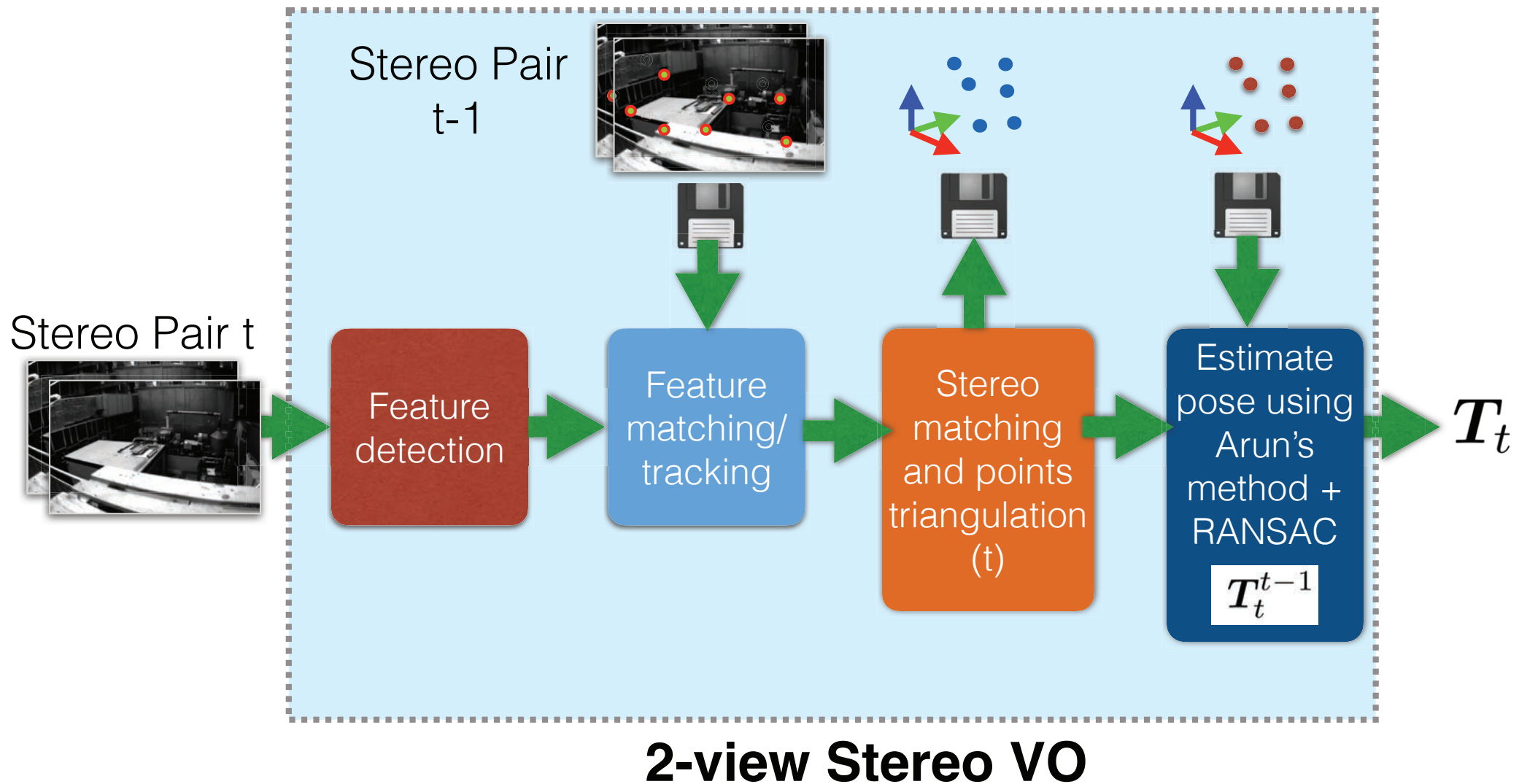




# Stereo Matching



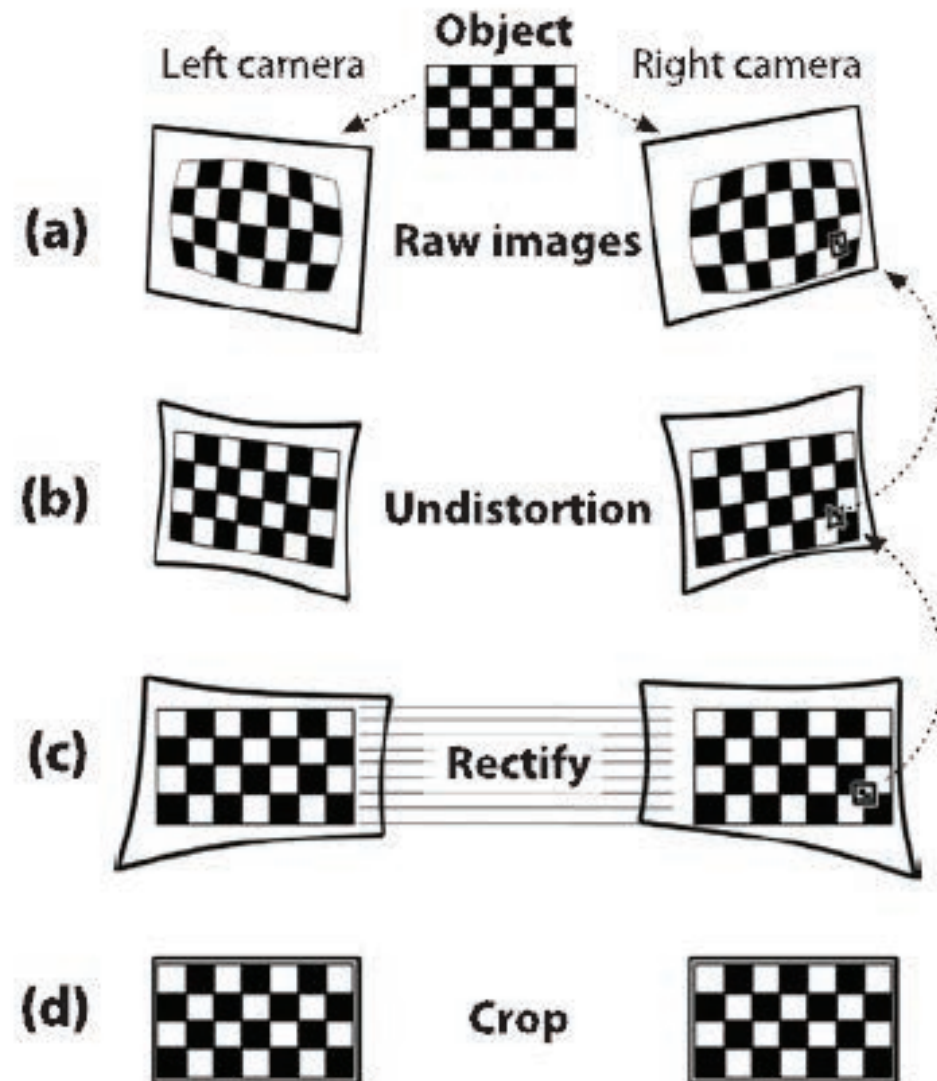
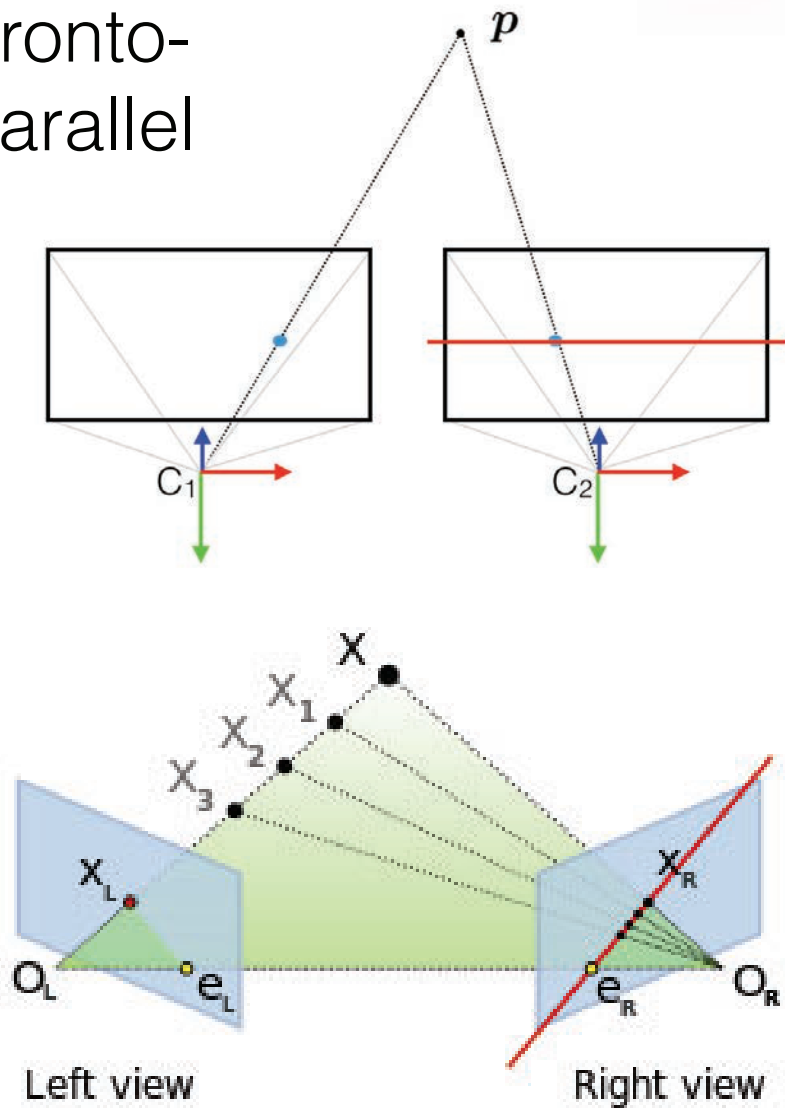
# Stereo VO with **3D-3D** Correspondences





# (Parenthesis on Stereo Matching)

Fronto-parallel

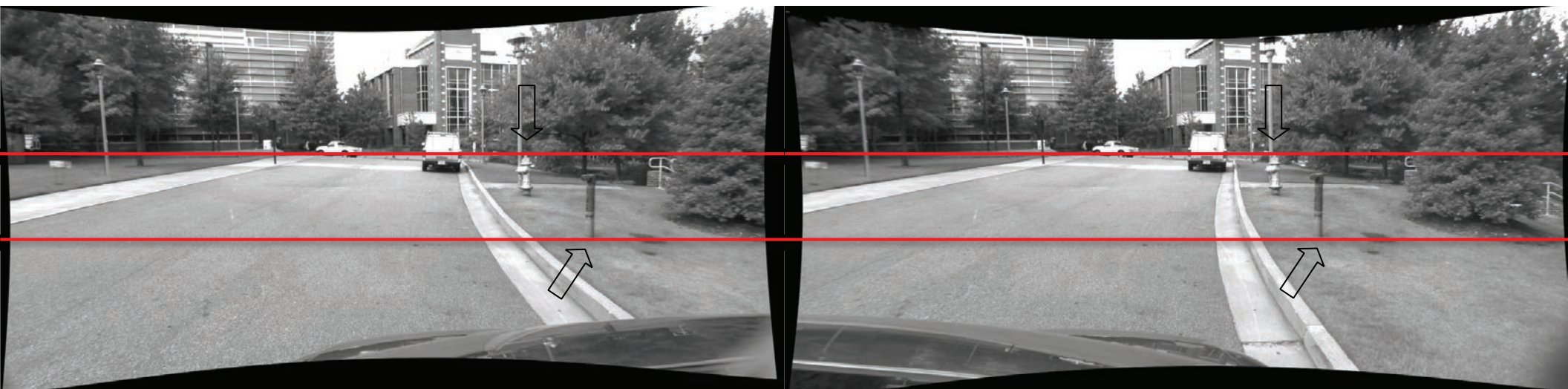
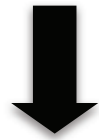
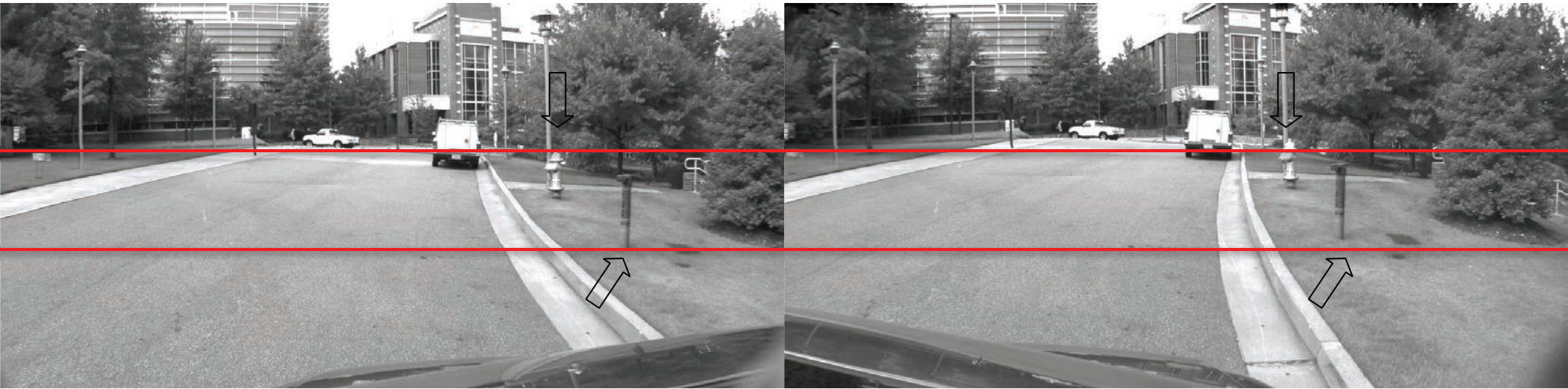


**OpenCV**: stereoRectify, initUndistortRectifyMap



# (Parenthesis on Stereo Matching)

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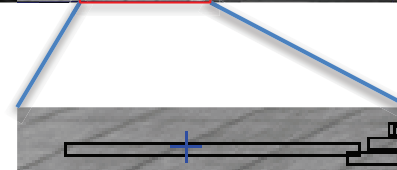
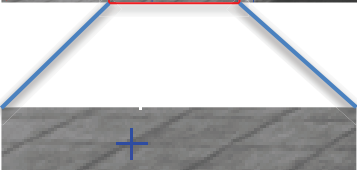
# (Parenthesis on Stereo Matching)

After **rectification**, we can restrict search for left-right matches to horizontal lines

Left image

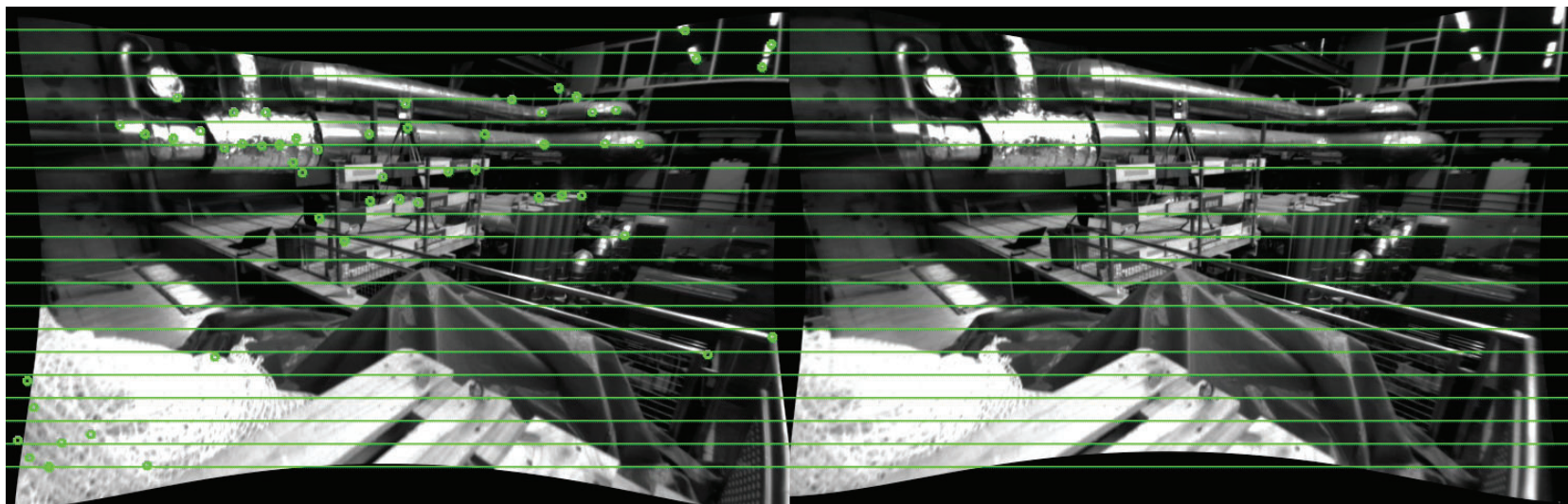


Right image



[courtesy of Frank Dellaert and Pablo Alcantarilla]

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# Comparing VO approaches

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**Drift** (error accumulation):

$$\mathbf{T}_0 = \mathbf{I}_4$$

$$\mathbf{T}_1 = \mathbf{T}_0 \mathbf{T}_1^0$$

$$\mathbf{T}_2 = \mathbf{T}_1 \mathbf{T}_2^1 = \mathbf{T}_0 \mathbf{T}_1^0 \mathbf{T}_2^1$$

⋮

$$\mathbf{T}_t = \mathbf{T}_{t-1} \mathbf{T}_t^{t-1} = \mathbf{T}_0 \mathbf{T}_1^0 \mathbf{T}_2^1 \cdots \mathbf{T}_t^{t-1}$$

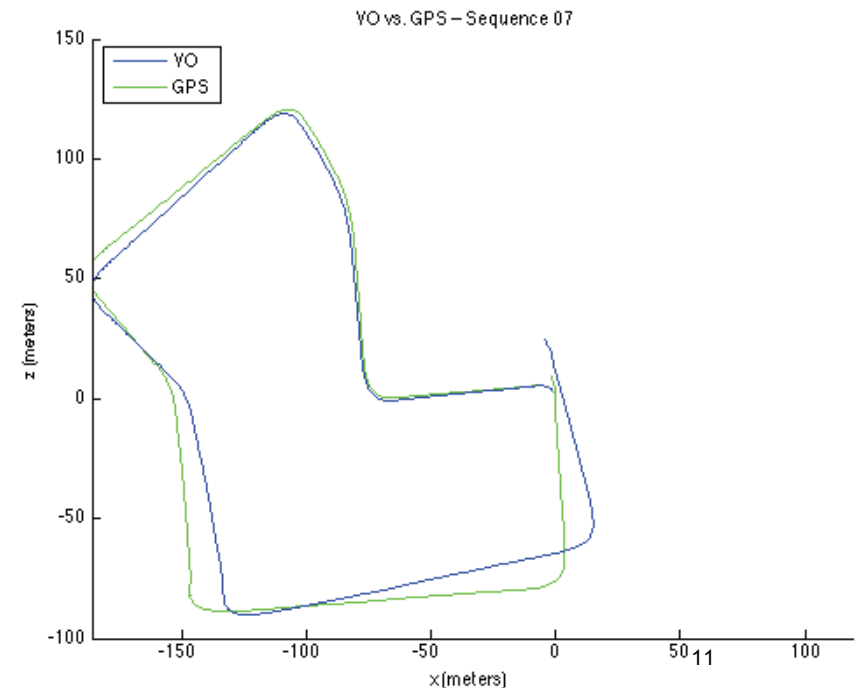
**Mono VO:**

- 5-point method accurate

**Stereo VO:**

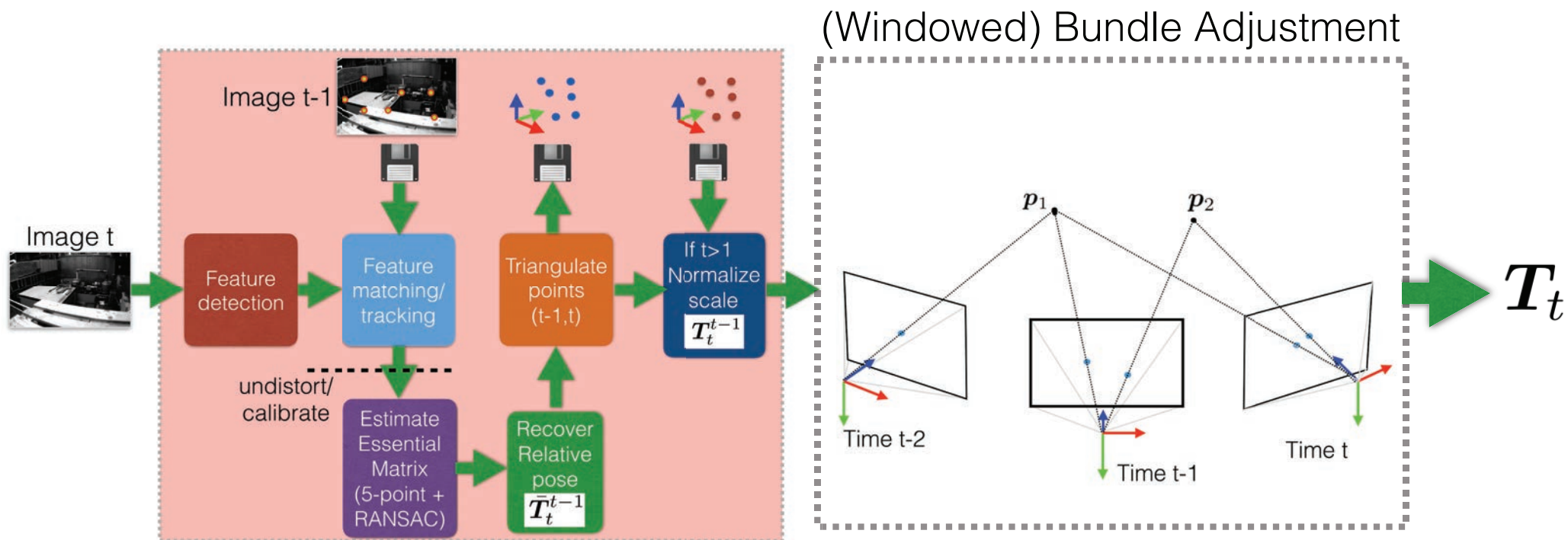
- scale

**Can we do better?**





# Refinement: Bundle Adjustment

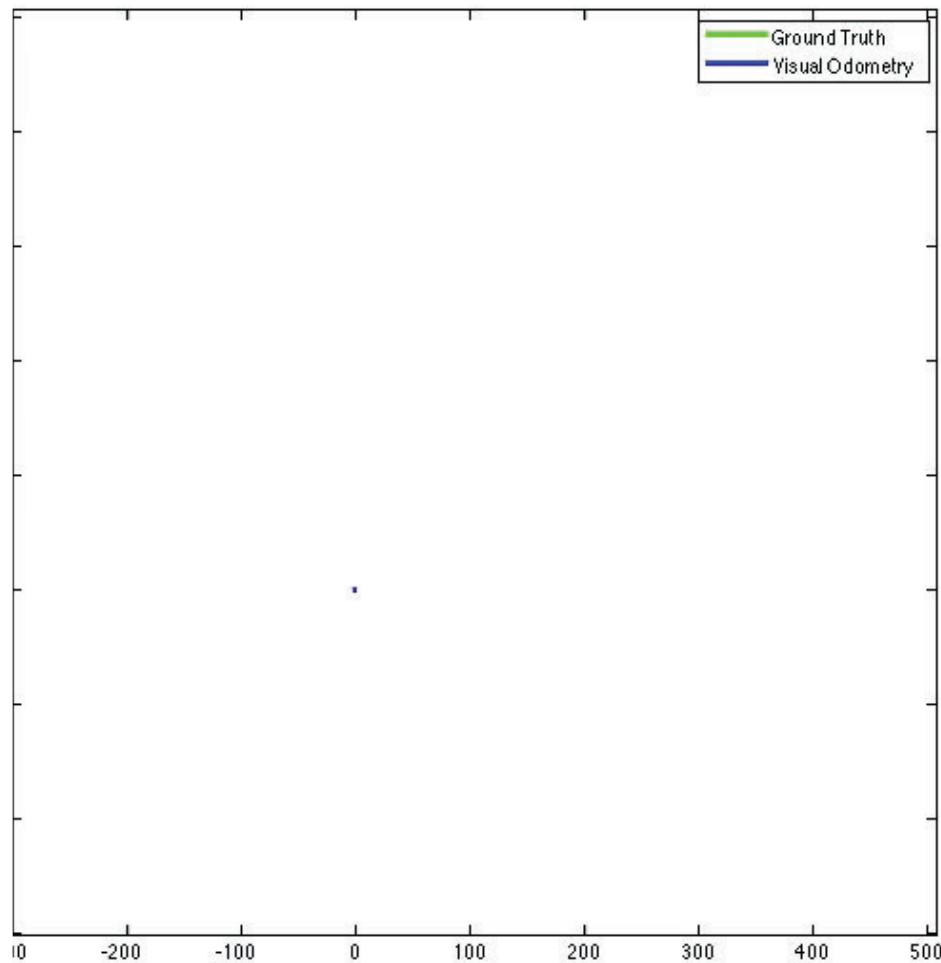


**Windowed Bundle Adjustment:** optimization of the most recent camera poses and points via non-linear least squares

$$\min_{\mathbf{T}_i, i=1, \dots, N_C} \min_{\mathbf{p}_k, k=1, \dots, N} \sum_{k=1}^N \sum_{i \in \mathcal{C}_k} \|\mathbf{x}_{k,i} - \pi(\mathbf{T}_i, \mathbf{p}_k)\|^2$$

Can be applied to all the pipelines discussed today

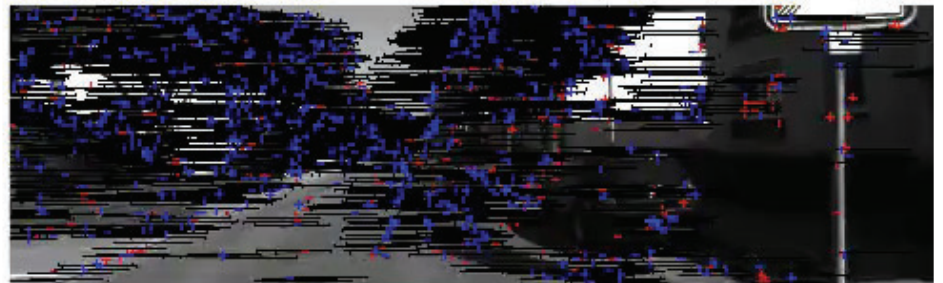
# Stereo VO example (2)



Left Camera



Right Camera



Frame 1



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Typical drifts: 0.1% to 2% of trajectory travelled

# Challenges for VO (1/3): Illumination and Features

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Feature detection,  
tracking,  
matching ...





# Challenges for VO (2/3): Dynamic Scenes

- Dynamic, crowded scenes present a real challenge
- Can't rely on RANSAC to always recover the correct inliers
- Example: Large van "steals" inlier set in passing



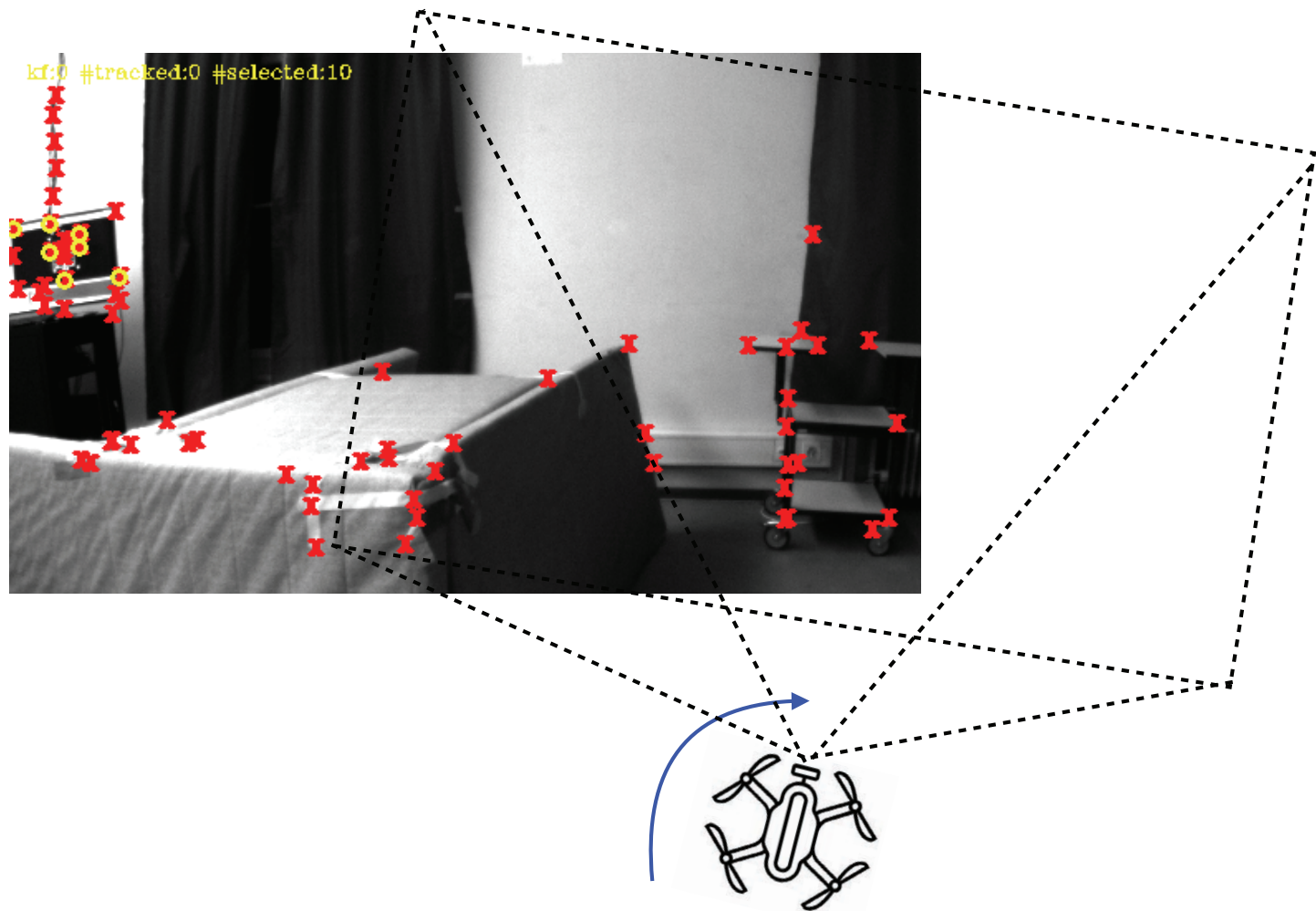
Inliers Outliers

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# Challenges for VO (3/3): Fast Motion

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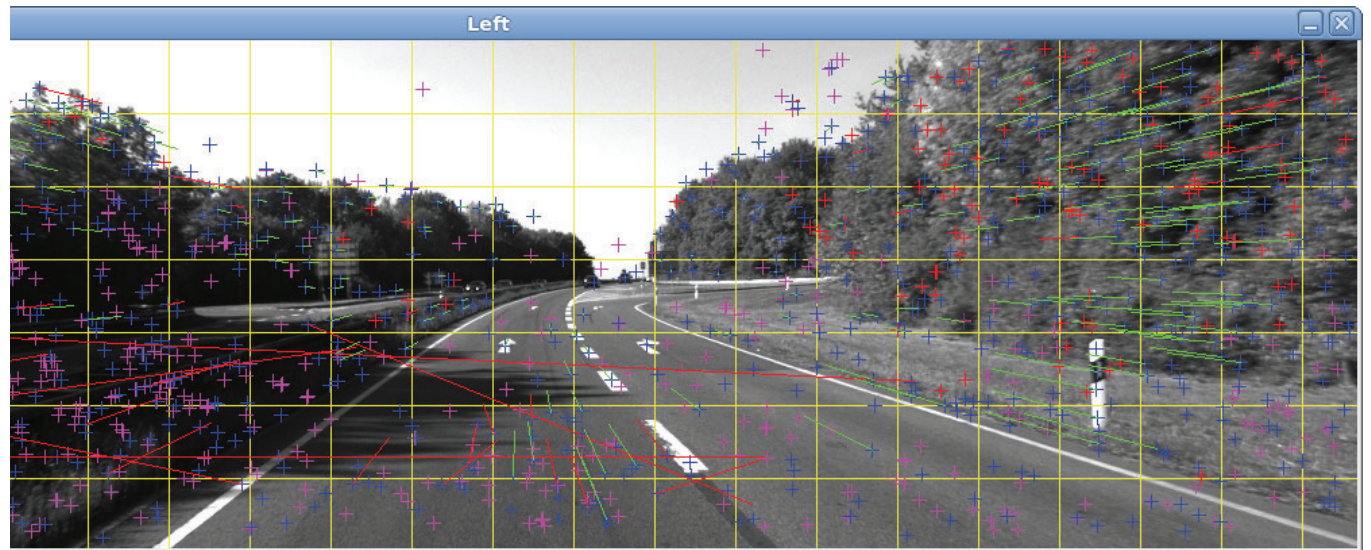
Need good overlap between consecutive images



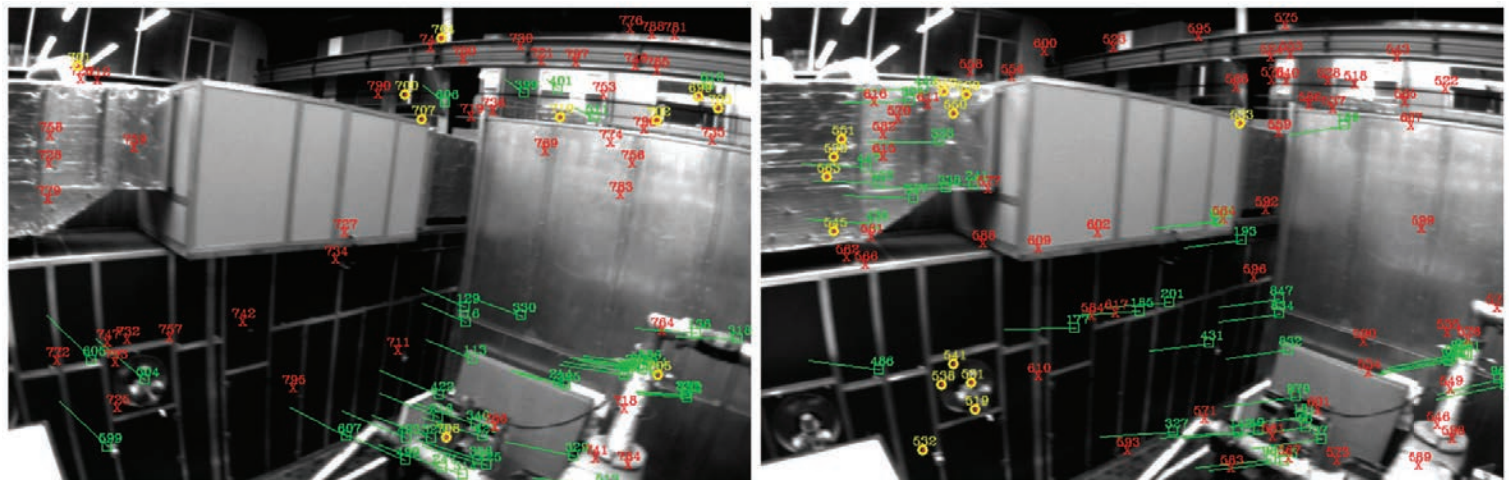
Robot speed, camera framerate, ...

# VO Tricks (1/2): Feature Distribution

Feature Binning:



Attention & Anticipation:  
(Carlone '17)

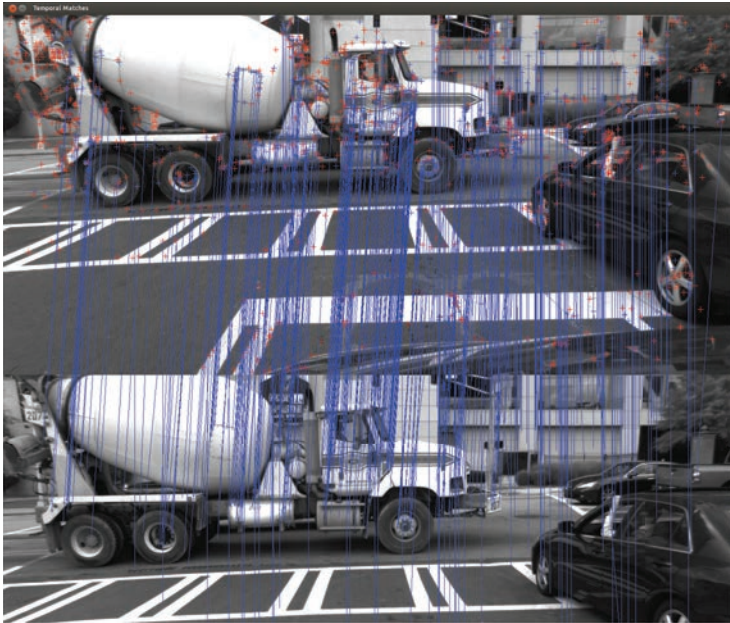


select features depending on motion of the robot <sup>17</sup>



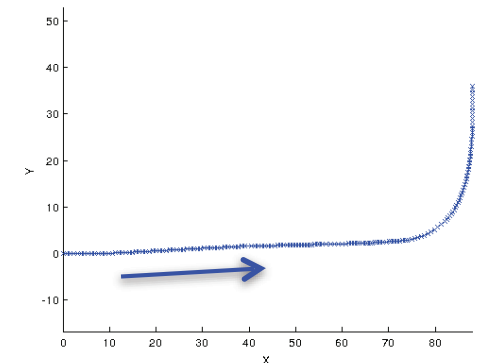
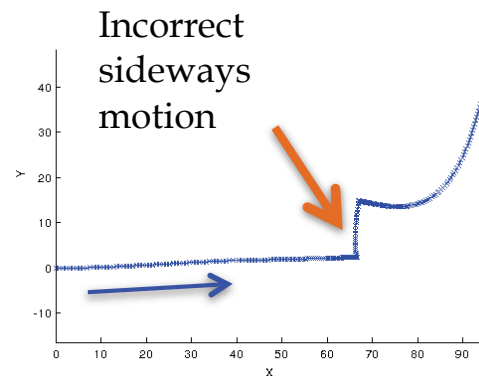
# VO Tricks (2/2): Domain Knowledge and Keyframes

- Stereo VO Example: Cross-traffic while waiting to turn left at light



Only accept incremental pose if:

- Translation  $> 0.5\text{m}$
- Dominant direction is forward

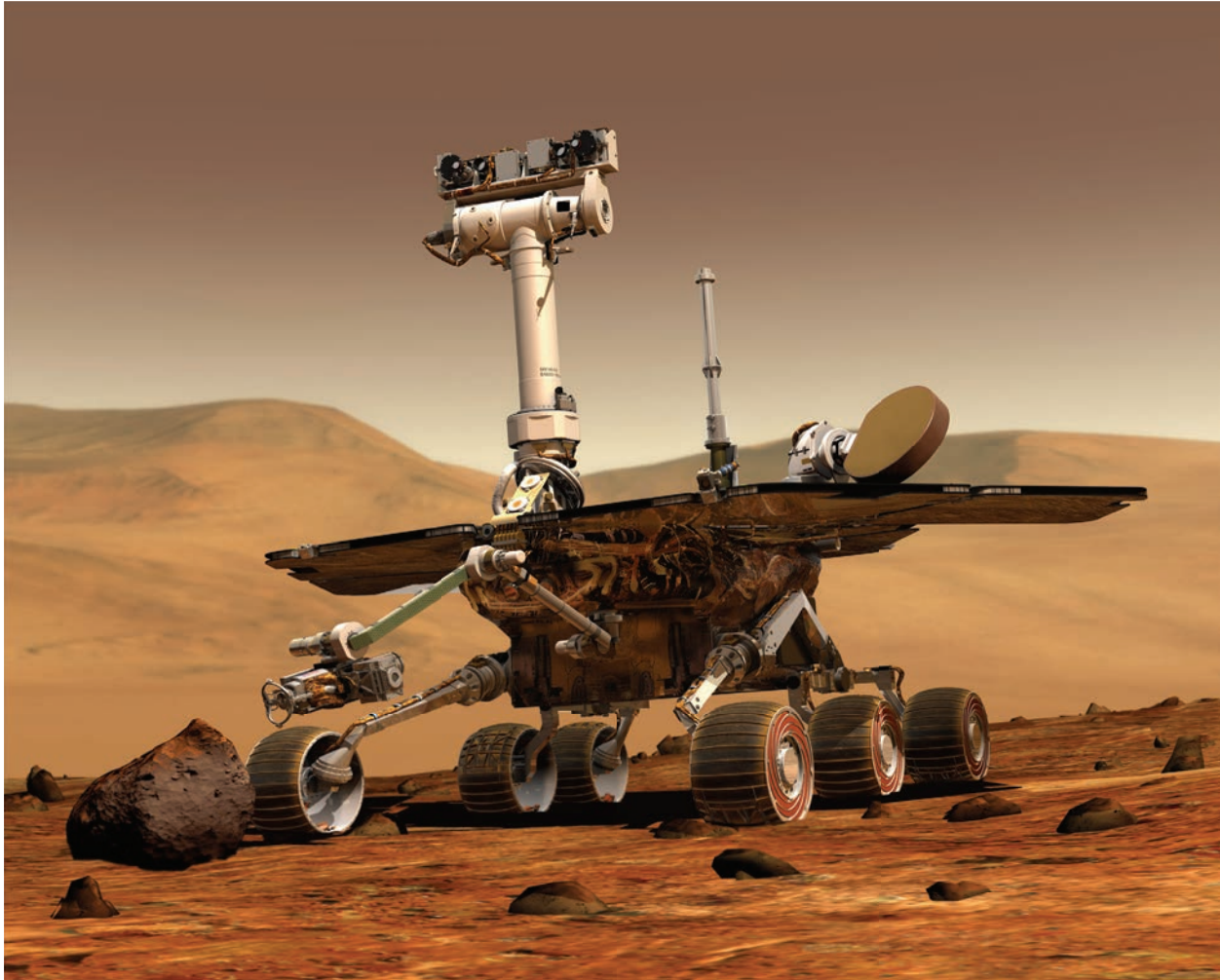


Without keyframing

With keyframing

# Stereo VO example (1)

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Source: public domain. Courtesy of NASA/JPL/Cornell University.

## **Spirit and Opportunity Mars rovers:**

- stereo VO
- 20-MHz CPU
- up to three minutes for 2-view VO
- Drift  $\sim 0.5\%$  of trajectory travelled

Earlier implementation: Moravec's PhD Thesis (1980)

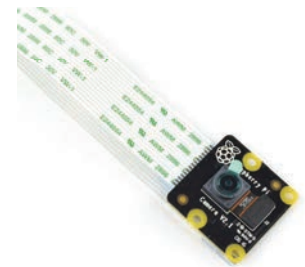
# Beyond VO

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How to get scale and improve robustness?

add more sensors!

- ▶ wheel odometry
- ▶ GPS
- ▶ Lidar
- ▶ Inertial Measurement Unit (IMU)



830g

160g

4g

3g

8 W

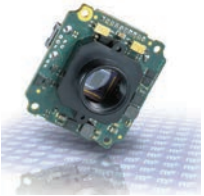
2.5 W

0.3W

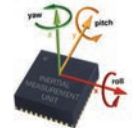
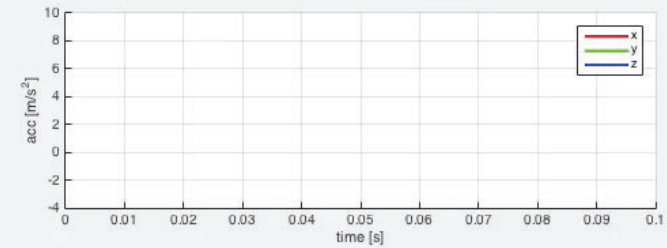
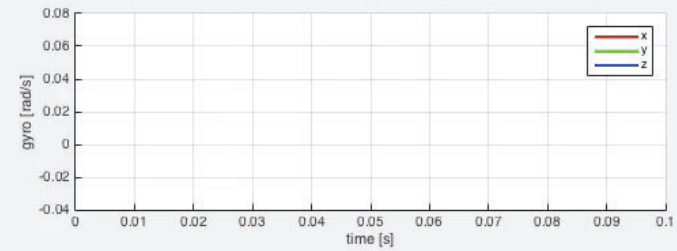
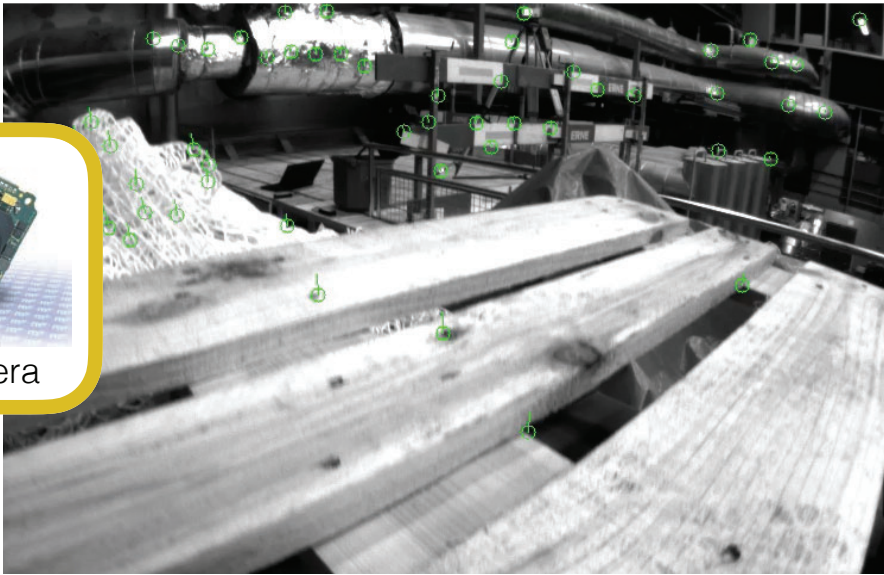
~1 W



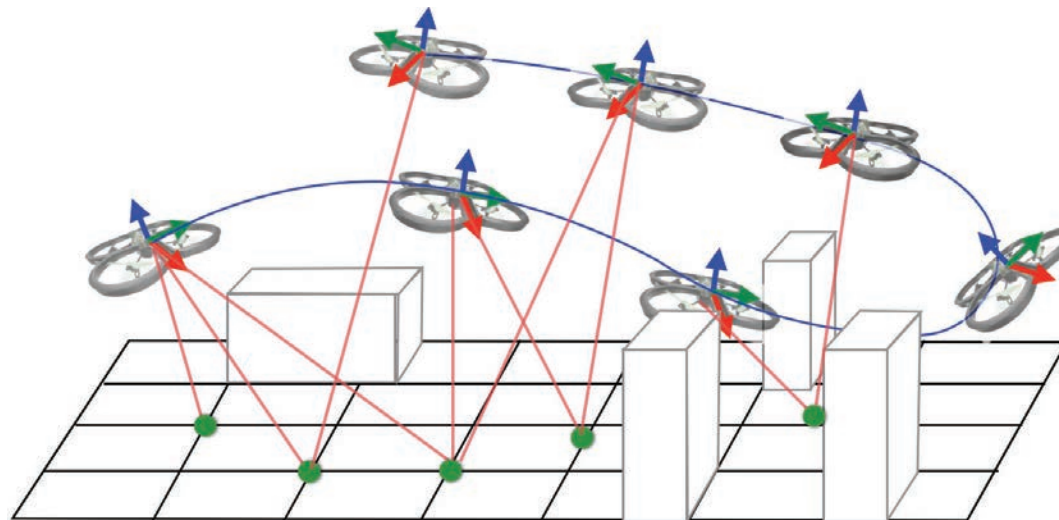
# Visual-Inertial Navigation (VIN)



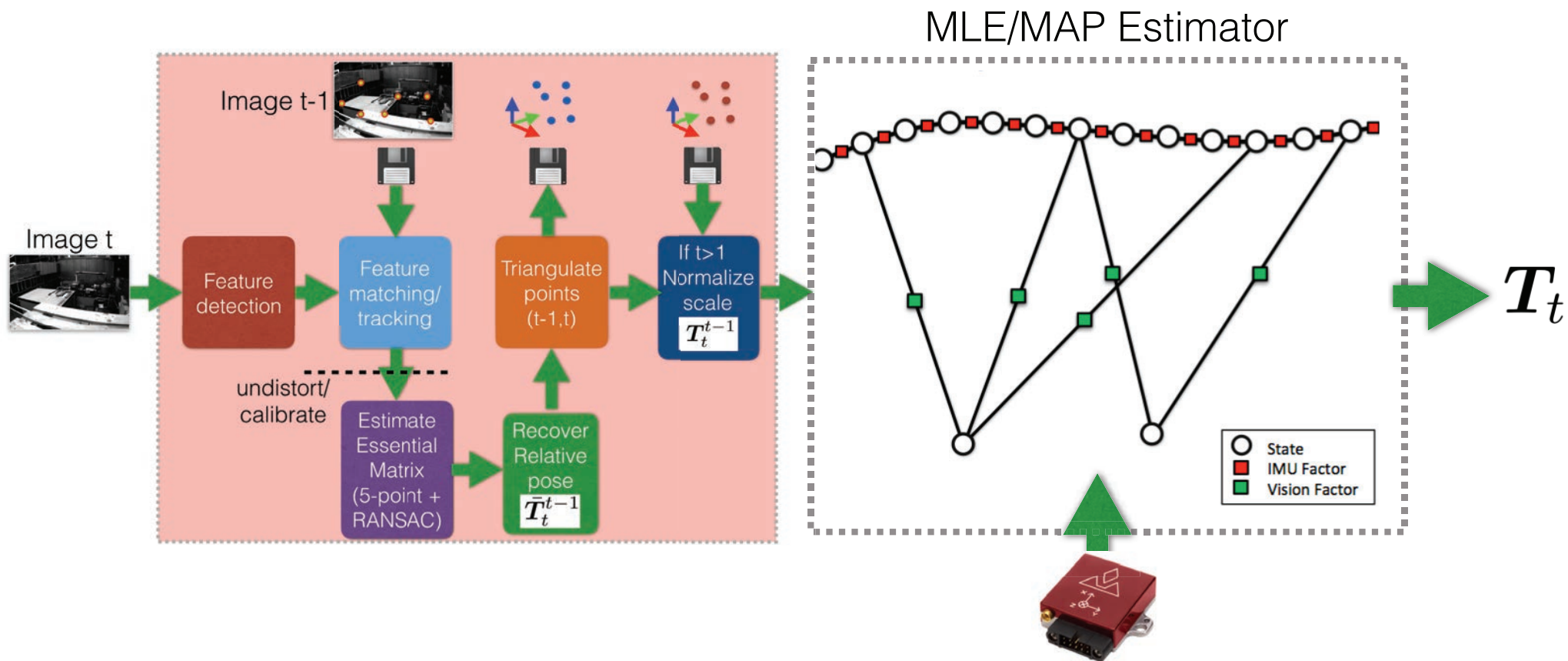
camera



Inertial Measurement Unit (IMU)



# Visual-Inertial Odometry



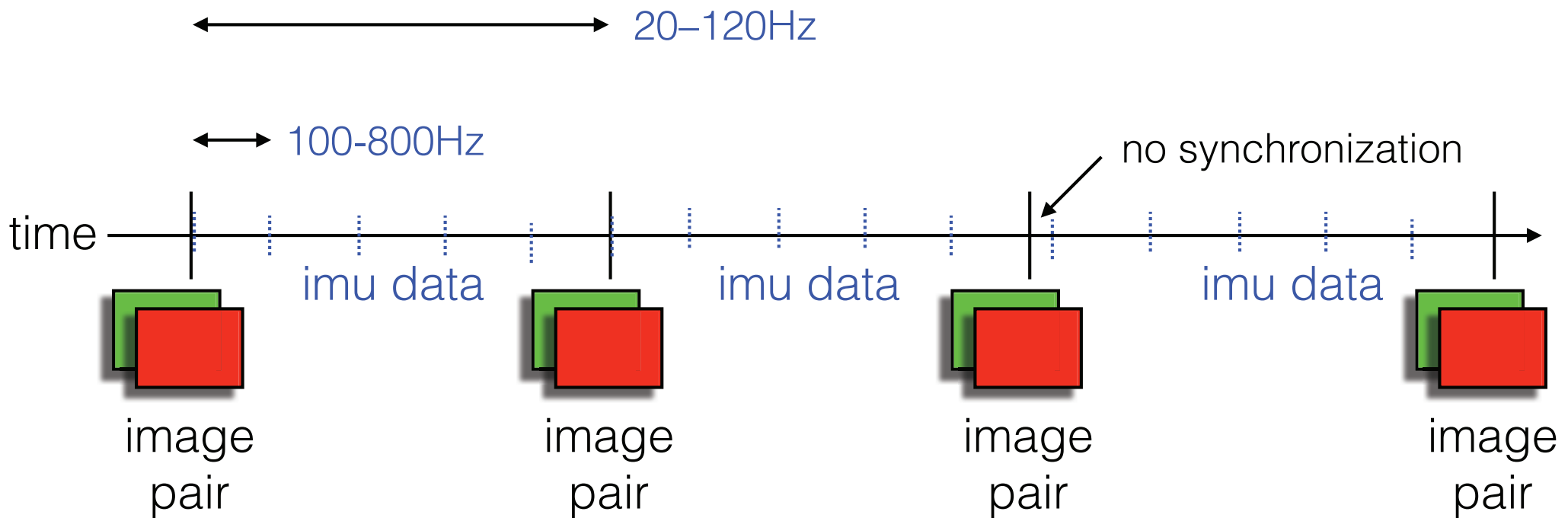
Camera factors

Imu factors

$$\min_{\mathbf{T}_i, i=1, \dots, N_C} \min_{\mathbf{p}_k, k=1, \dots, N} \sum_{k=1}^N \sum_{i \in \mathcal{C}_k} \|\mathbf{x}_{k,i} - \pi(\mathbf{T}_i, \mathbf{p}_k)\|^2 + \sum_{i=1, \dots, N_C-1} \|r_{\text{imu}}(\mathbf{T}_i, \mathbf{T}_{i+1}, \mathbf{v}_i, \mathbf{v}_{i+1}, \mathbf{b}_i, \mathbf{b}_{i+1})\|^2$$

Need to include velocities and IMU biases in the state ...

# Visual-Inertial Odometry

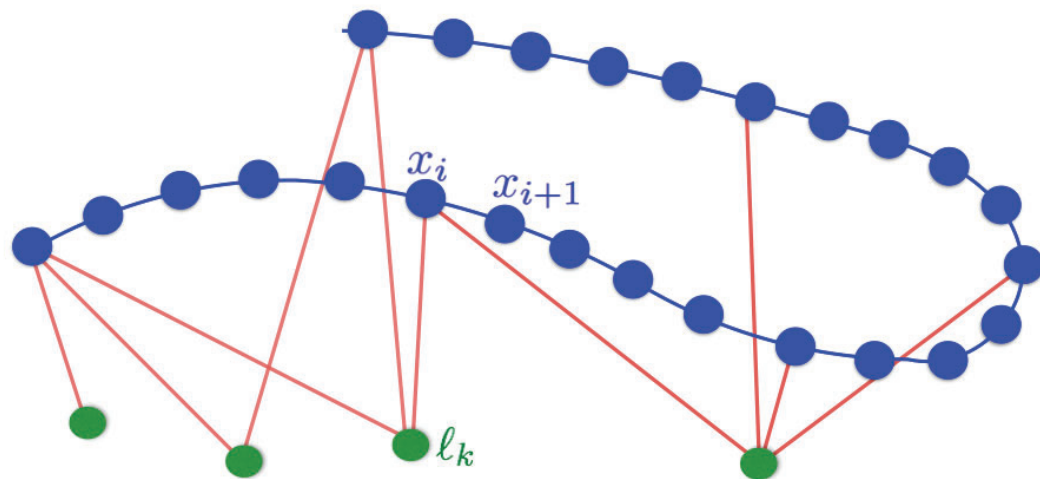


## Challenges:

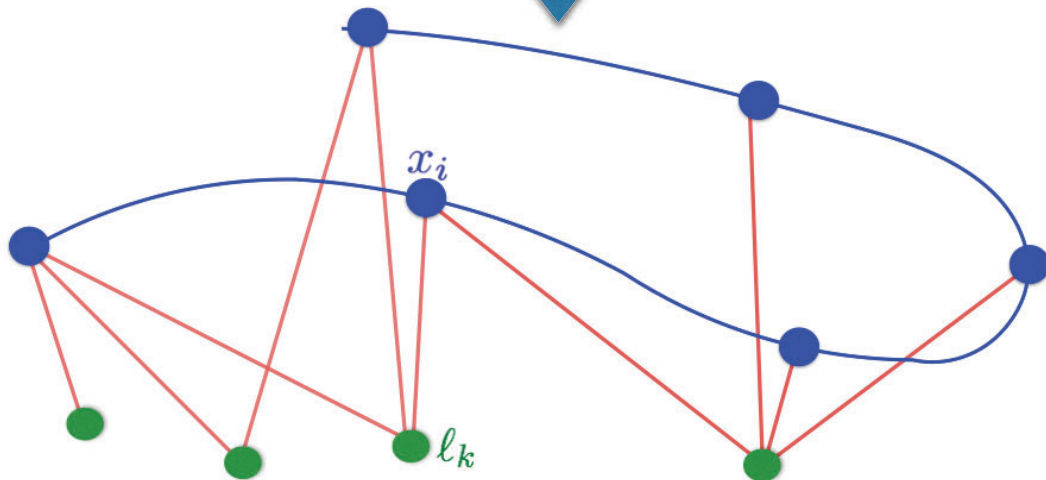
- IMU measurements arrive at high-rate ( $\sim 200\text{Hz}$ )  $\Rightarrow$  **IMU preintegration**
- camera observes hundreds of landmarks per frame  $\Rightarrow$  **structureless vision factors**
- need to solve optimization problem quickly



# Pre-integration



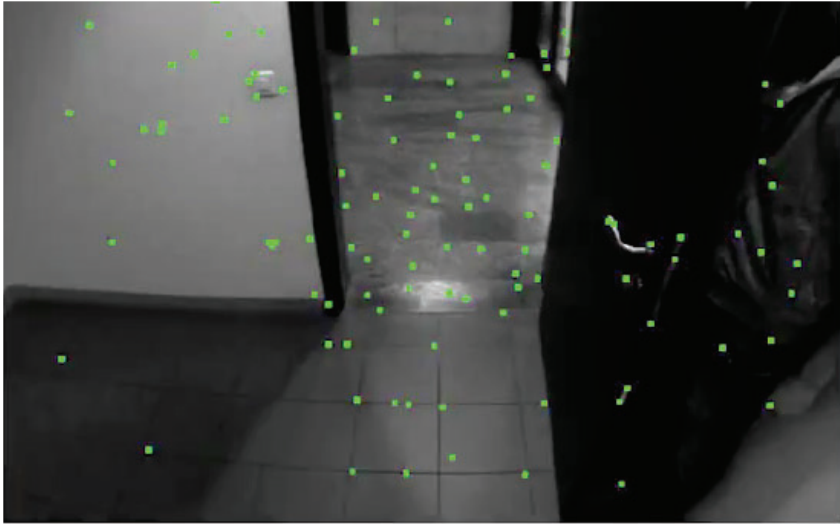
After 10 seconds, original problem has  $\sim 10^4$  states



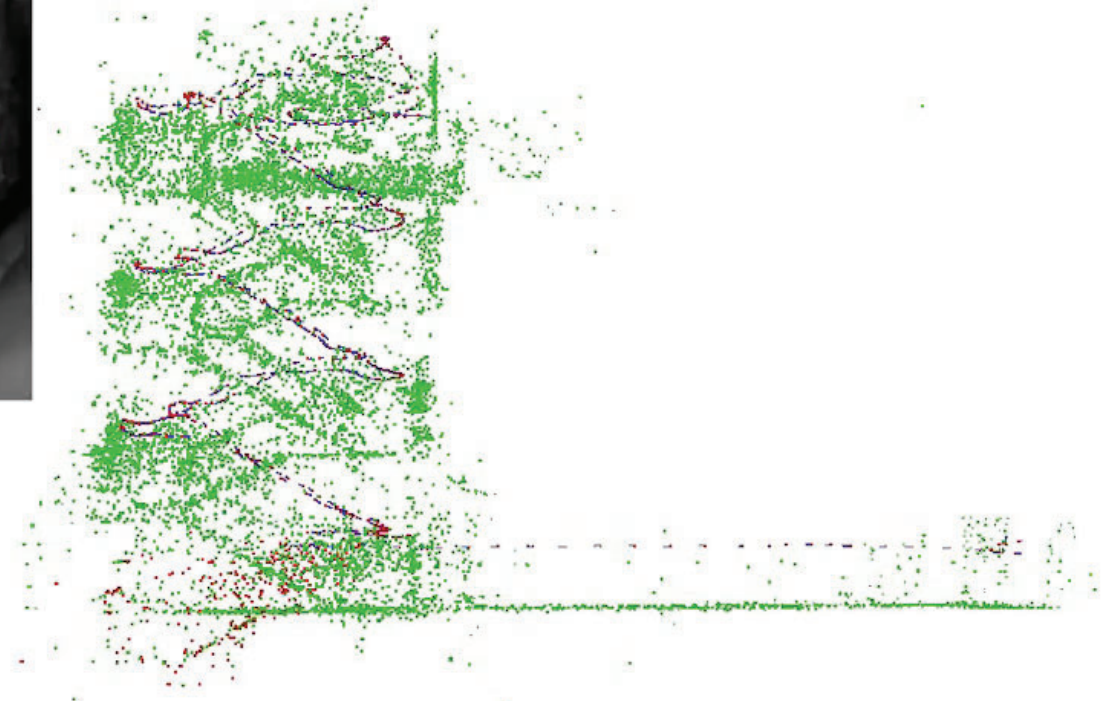
After 10 seconds, preintegrated problem has  $\sim 10^2$  states

# Visual-Inertial Odometry

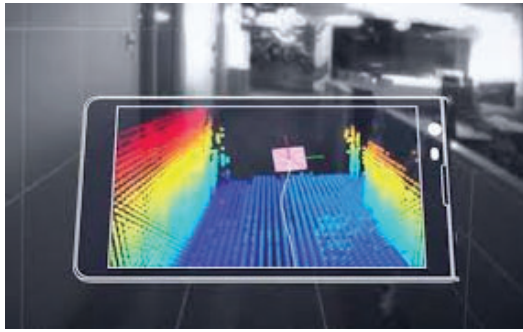
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Hand-held  
sensor



# Recent Implementations / Products



2014

Reinvented as  
ARCore in 2017

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Oculus Rift

Announced in 2012.  
Acquired by  
Facebook in 2014

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Navion Chip  
2017

(<http://navion.mit.edu/>)

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Pokemon Go





# Beyond VO

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How to get scale and improve robustness?

add more sensors!

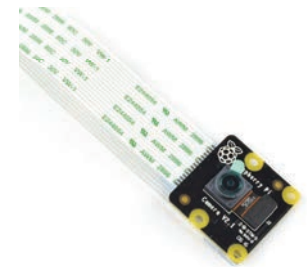
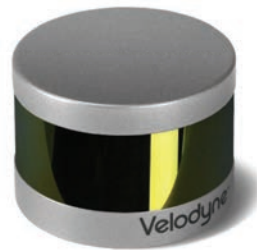
▶ wheel odometry

▶ GPS

▶ Lidar

▶ Inertial

Measurement  
Unit (IMU)



830g

160g

4g

3g

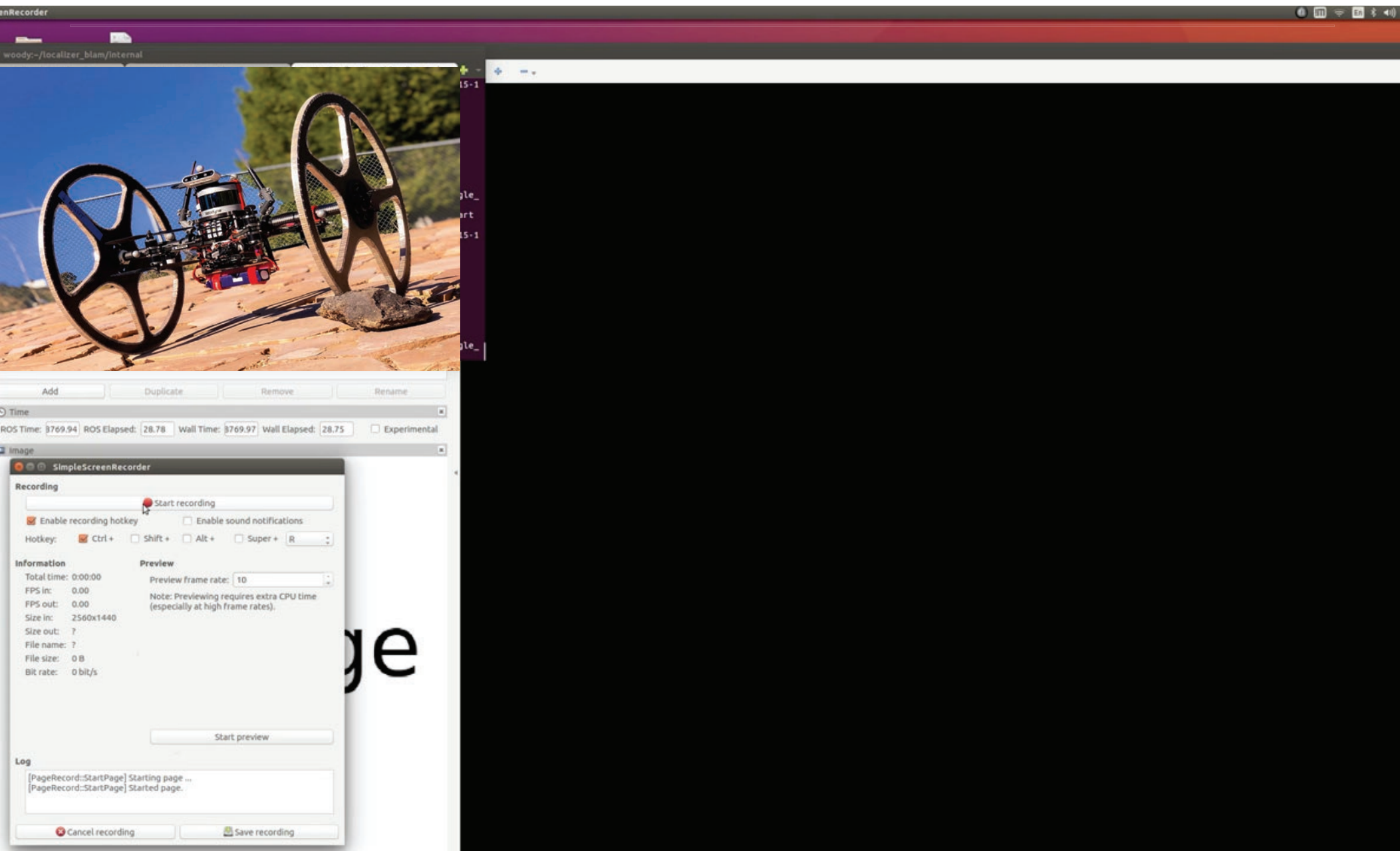
8 W

2.5 W

0.3W

~1 W

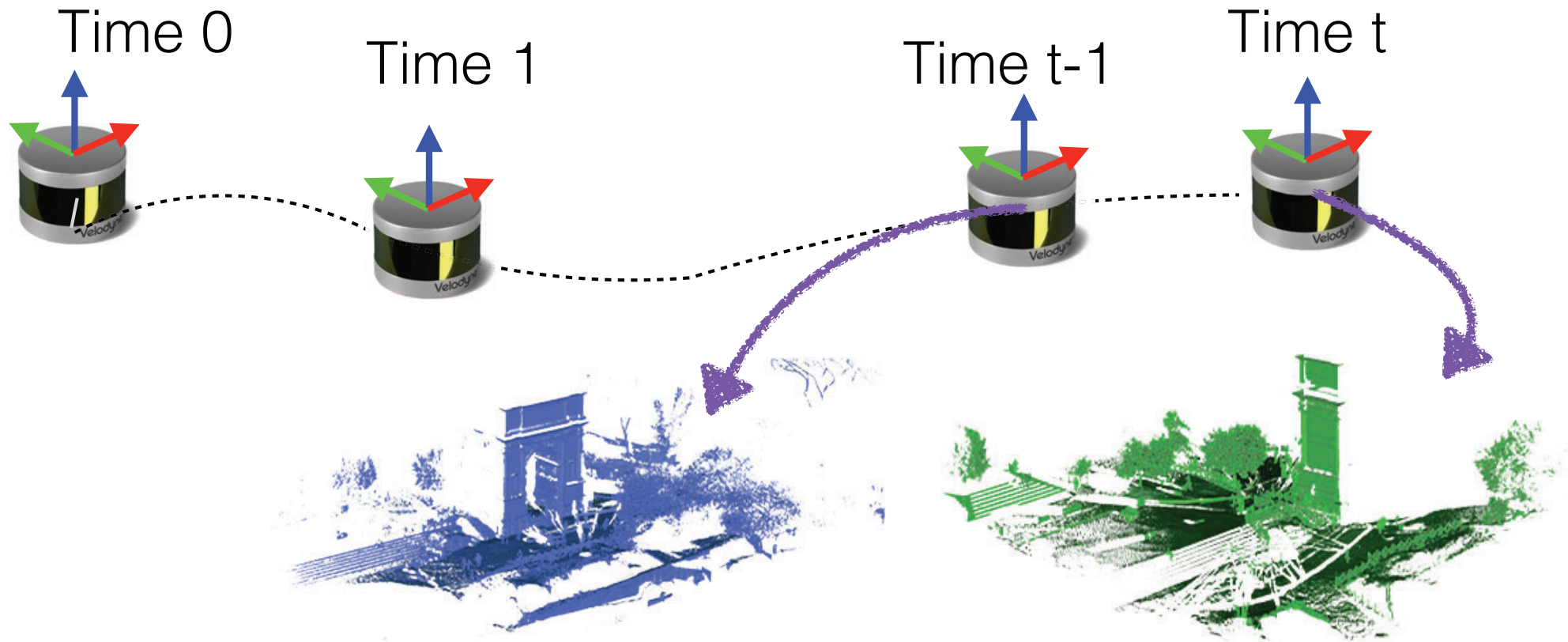
# Lidar Odometry & Lidar SLAM



**DARPA Subterranean Challenge**, in collaboration with JPL

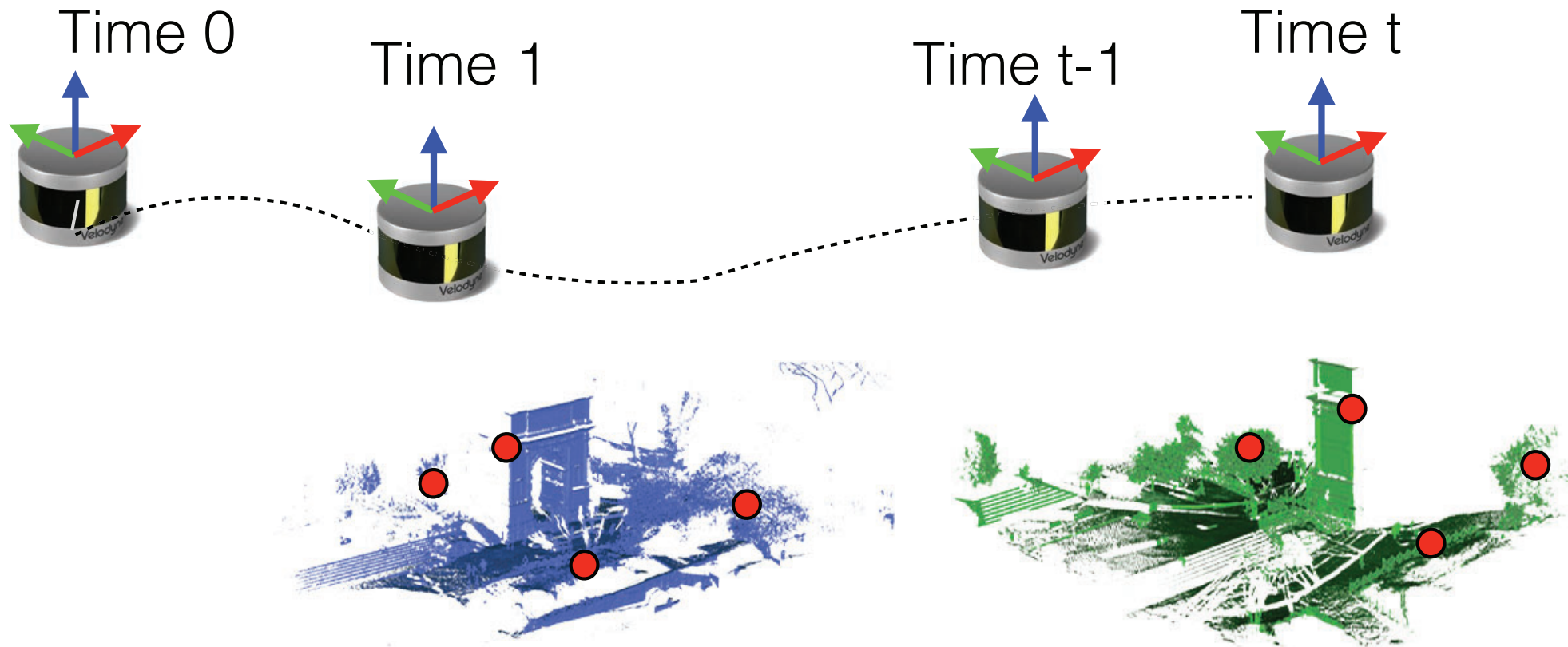
# Feature-based Lidar Odometry

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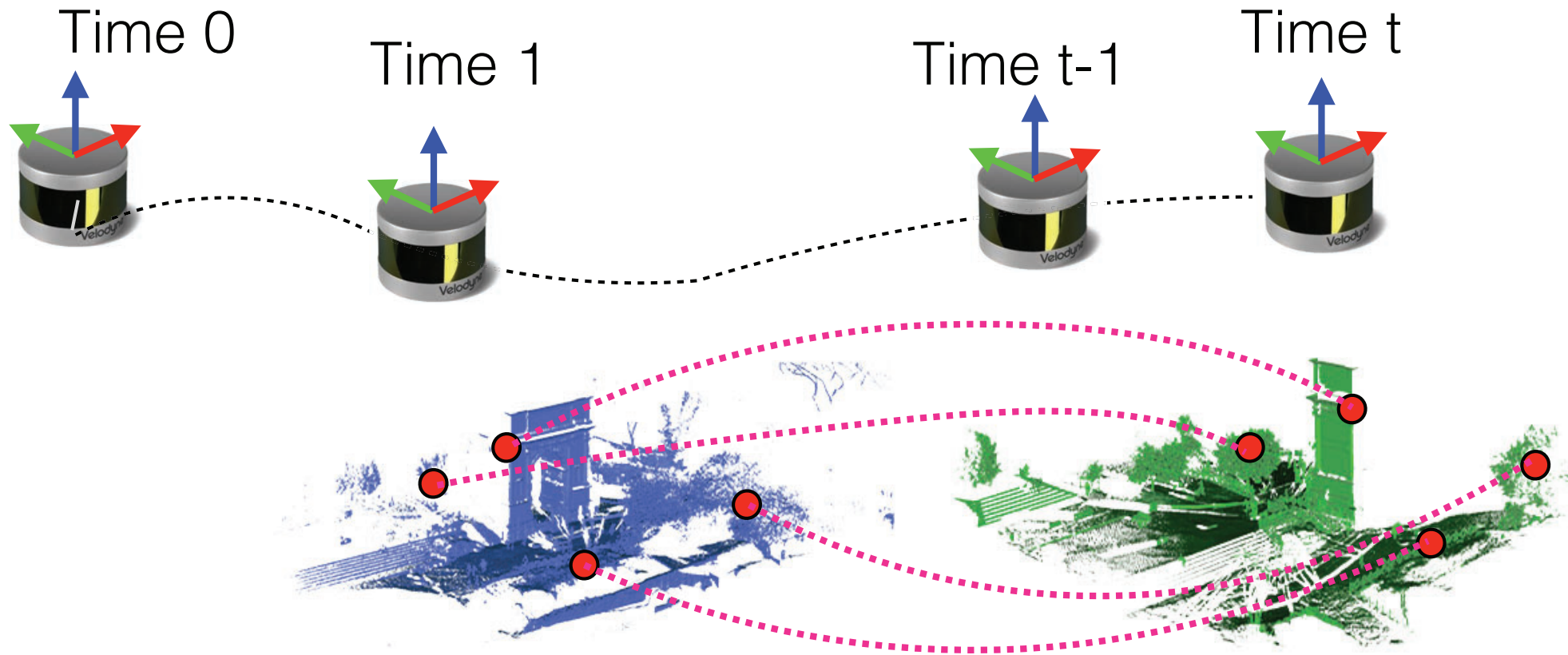
# Feature-based Lidar Odometry



**Registration:** compute relative pose between scans:

- extract features & descriptors
- use descriptors for matching
- compute relative pose

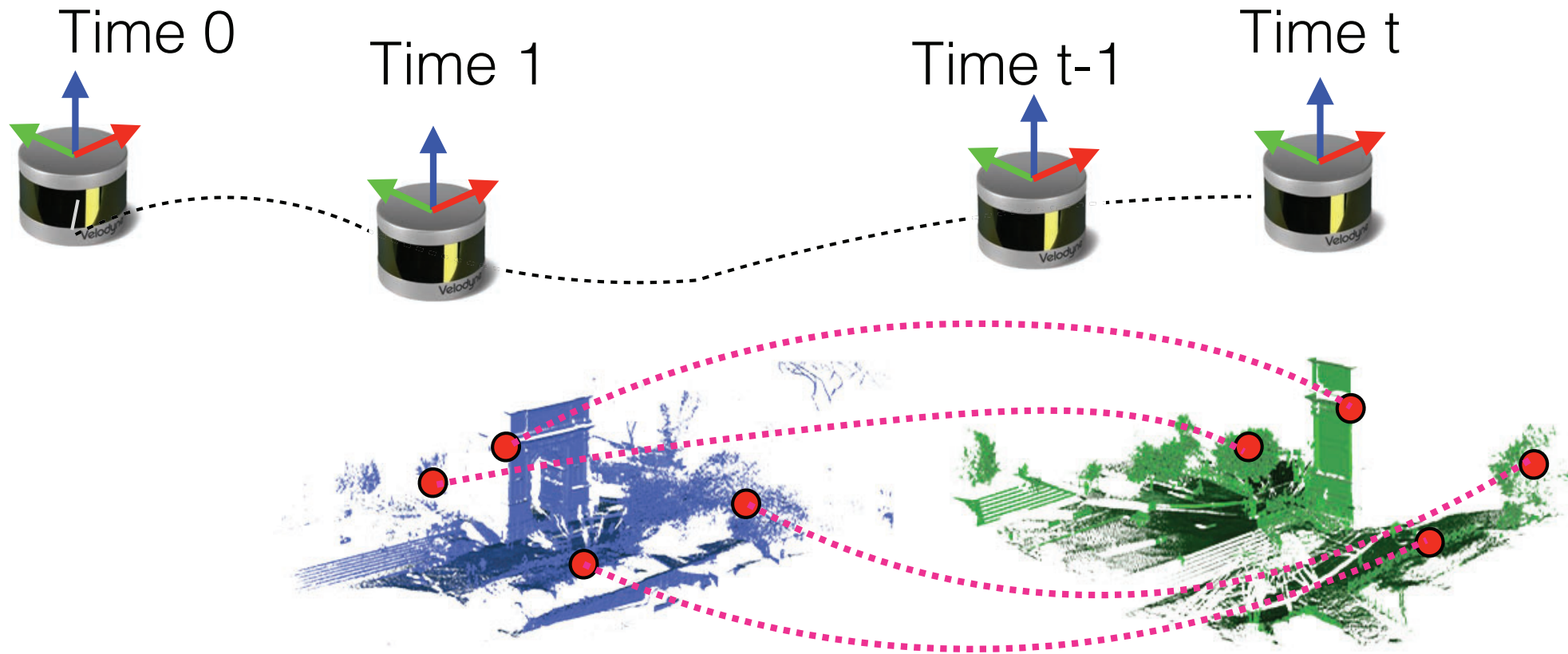
# Feature-based Lidar Odometry



**Registration:** compute relative pose between scans:

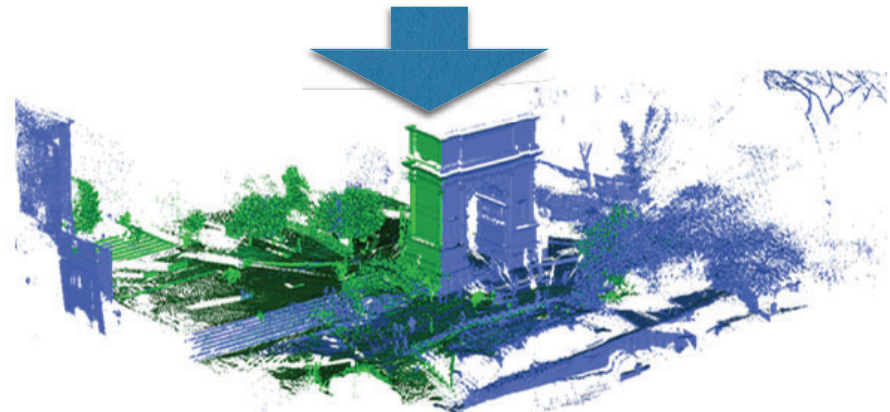
- extract features & descriptors
- use descriptors for matching
- compute relative pose

# Feature-based Lidar Odometry



**Registration:** compute relative pose between scans:

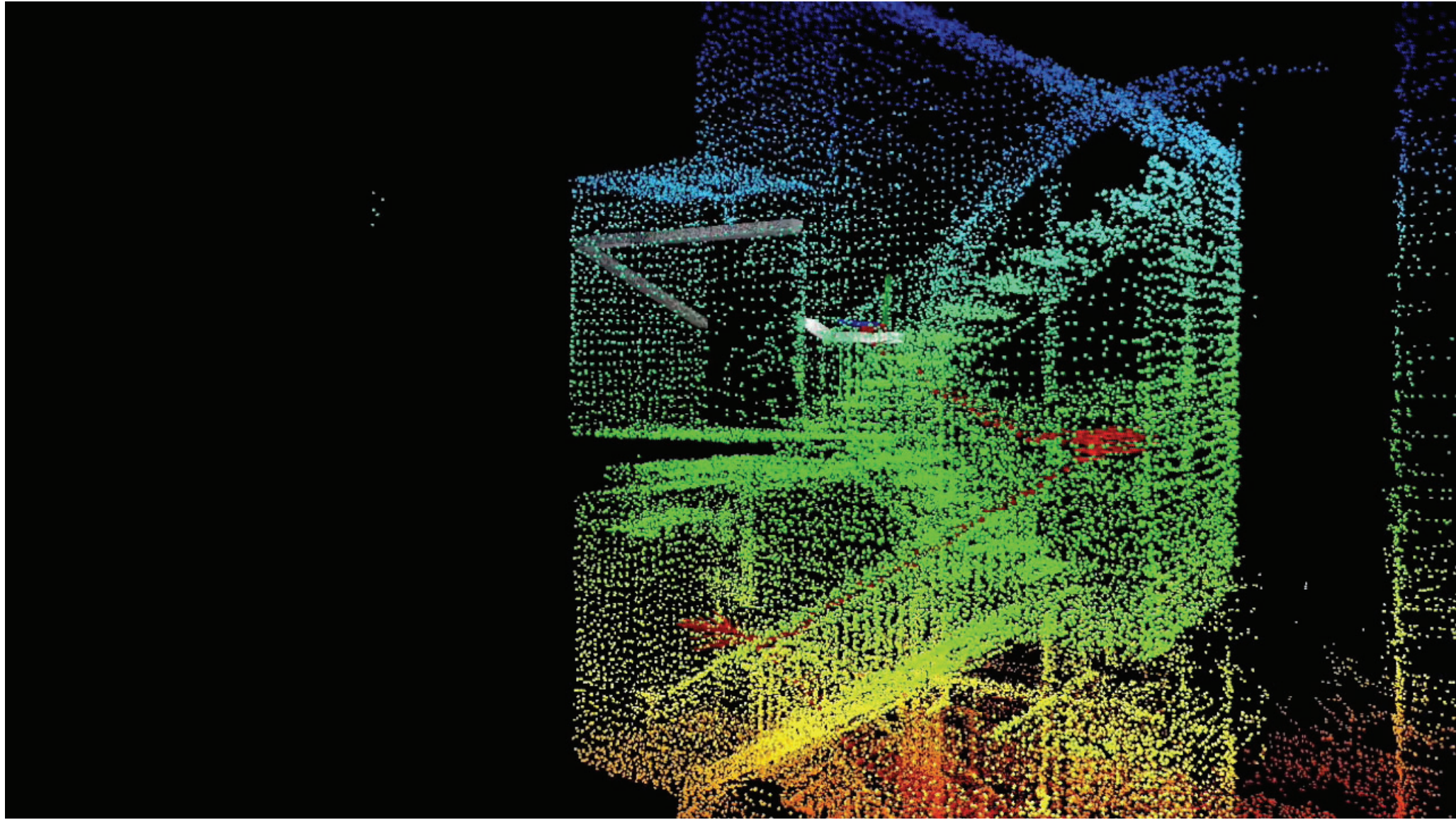
- extract features & descriptors
- use descriptors for matching
- compute relative pose





# Feature-based Lidar Odometry

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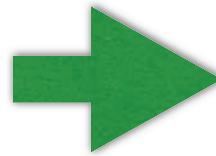
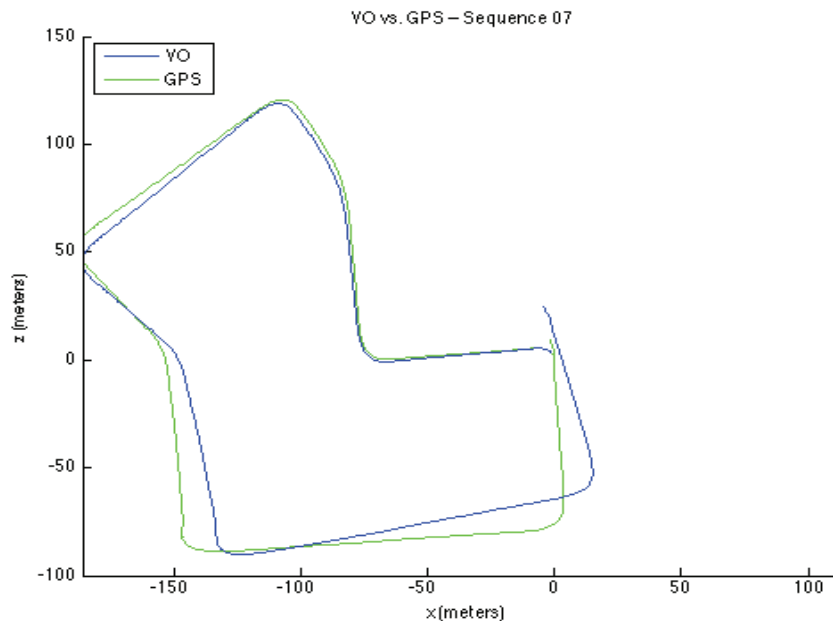


[Zhang and Singh: LOAM: Lidar Odometry and Mapping in Real-time, 2014]

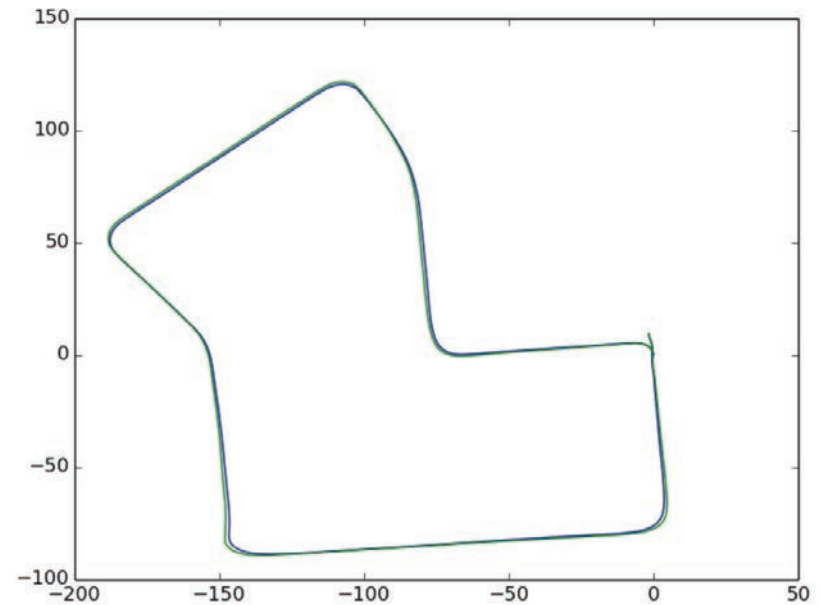
Other approaches: based on Iterative Closest Point (ICP)<sup>33</sup>

# Removing Drift via Loop Closure

Visual(-inertial) odometry



SLAM



SLAM requires:

- place recognition (loop closure detection)
- Re-detecting landmarks (e.g., objects)

Next lecture!

# Need for loop closure

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## ORB-SLAM

Raúl Mur-Artal, J. M. M. Montiel and Juan D. Tardós

{raulmur, josemari, tardos} @unizar.es



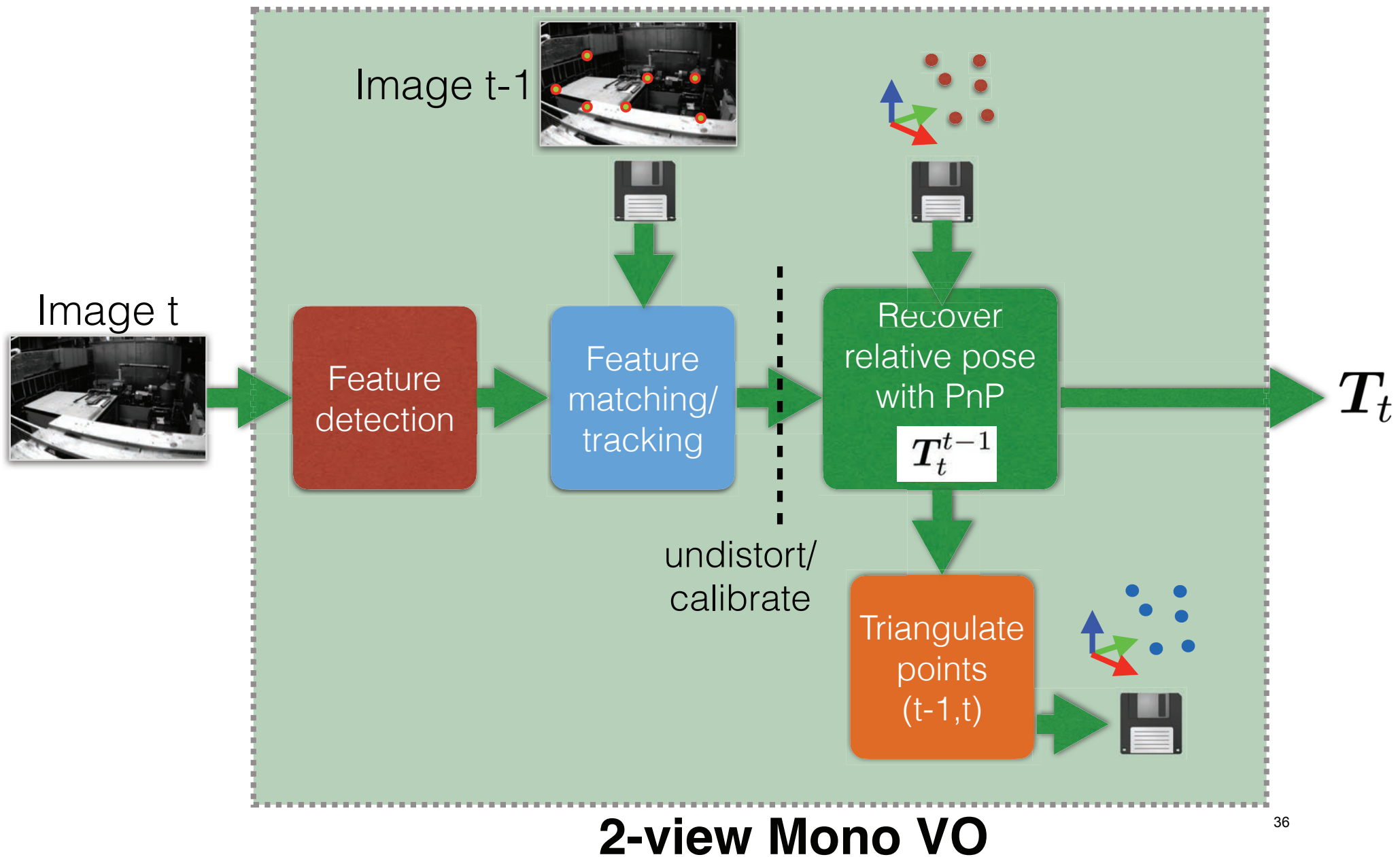
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en Ingeniería de Aragón  
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**Universidad**  
Zaragoza



# Monocular VO with **3D**-2D Correspondences



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Fall 2020

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